

Spherical Indexing of EBSD Patterns

Stuart Wright, René de Kloe

Outline

- Hough Based Indexing
- Forward Model Based Indexing
 - Dictionary indexing
 - **Spherical indexing**
 - application results
 - Refinement
 - improved angular resolution
 - resolving pseudo-symmetry
 - Extension of Spherical Indexing



Will Lenthe



Stuart Wright



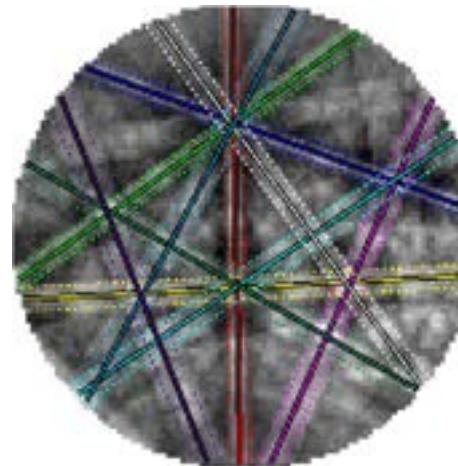
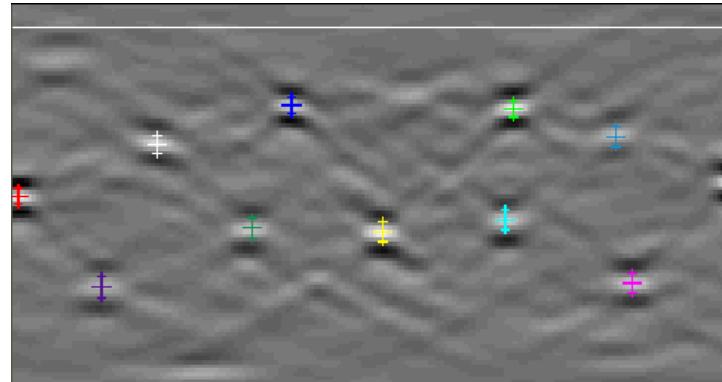
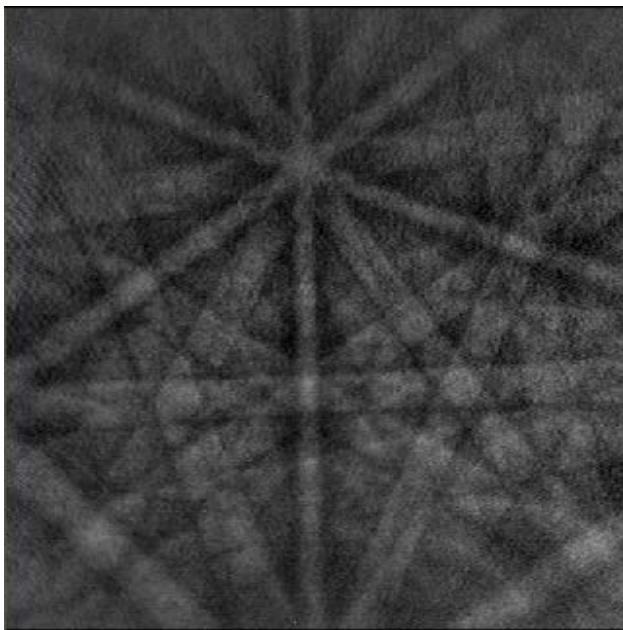
Matt Nowell



René de Kloe

Hough transform

N. C. Krieger-Lassen, K. Conradsen, and D. Juul-Jensen
(1992) "Image Processing Procedures for Analysis of
Electron Back Scattering Patterns", *Scanning Microscopy*, **6**,
115-121.

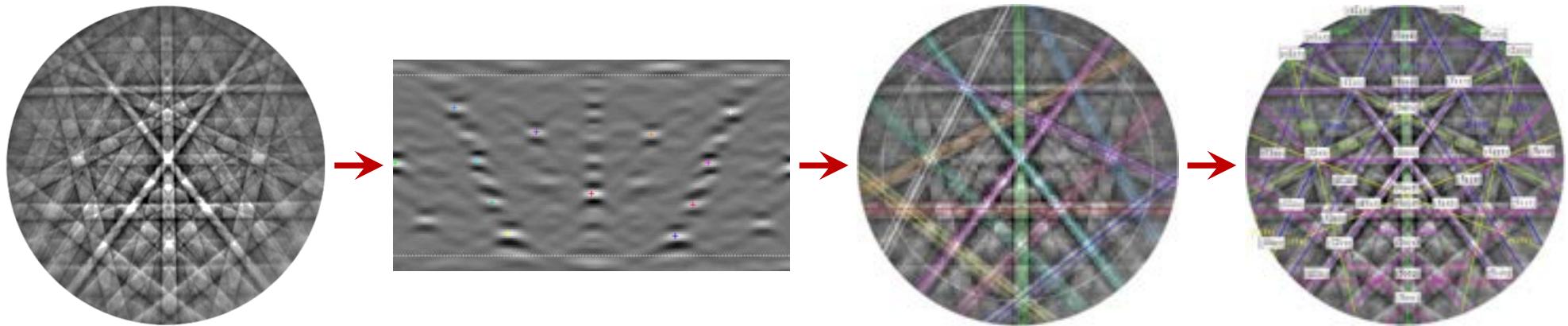


"Advances in Automatic EBSP Single Orientation Measurements"
K. Kunze, S.I. Wright, B.L. Adams
and D.J. Dingley. *Textures and Microstructures* **20**, 41-54 (1993).

Presented at *Microscale Texture of Materials Symposium, ASM/TMS Meeting*,
Cincinnati, Ohio, October 1991.

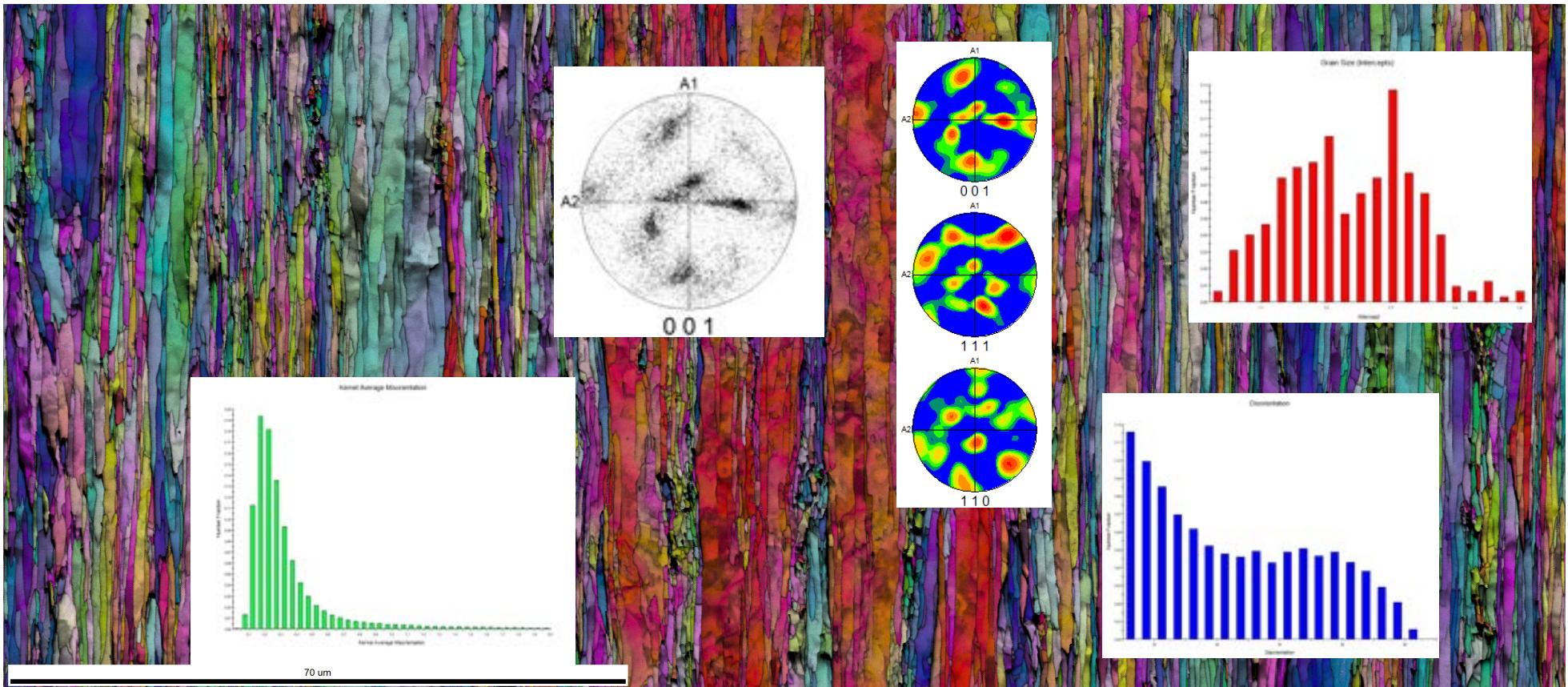
Hough transform and triplet indexing

- Hough-transform based indexing method
- Collect a pattern → detect the bands to “reconstruct” the pattern → match the interplanar angles against an (ideal) reference model → find a solution

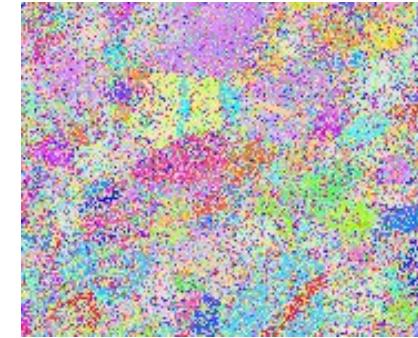
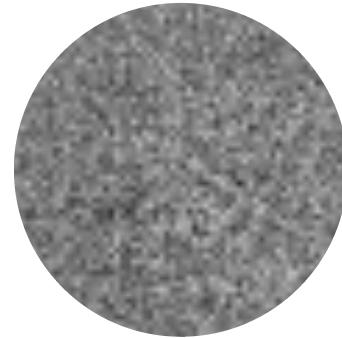
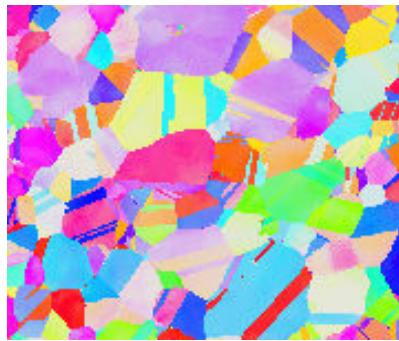
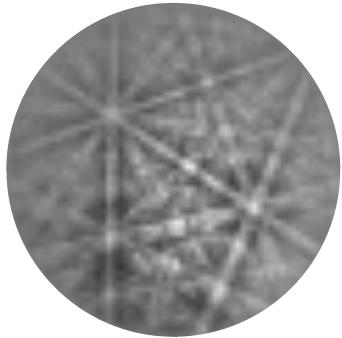


- Works very well but requires:
 - Consistent band detection
 - Detecting enough bands
 - Accurate band direction determination
 - Minimal pattern shadowing

Example → heavily deformed Mo sample with triplet indexing



Hough transform and triplet indexing

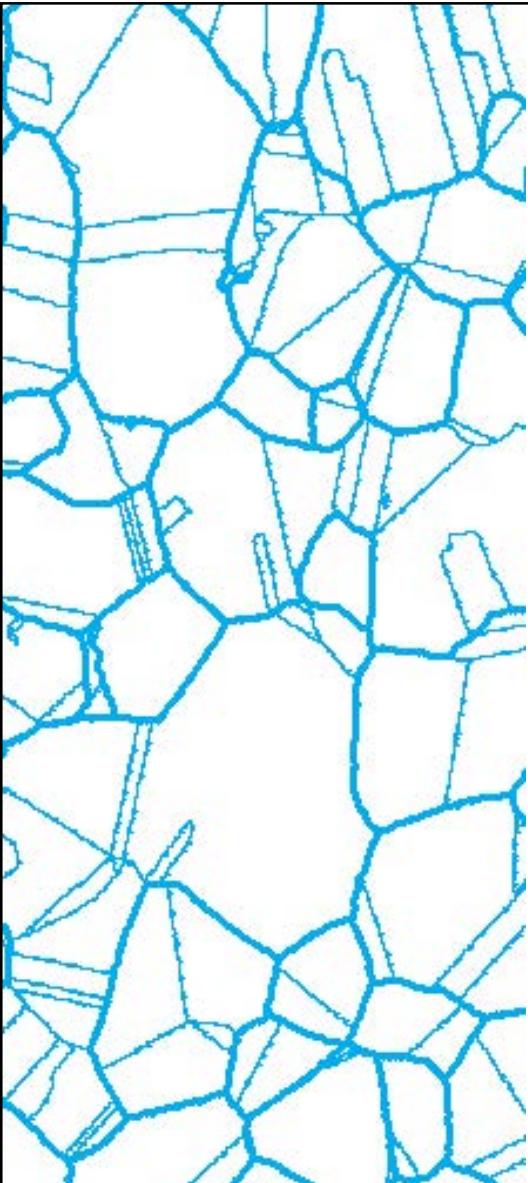


- Pros:

- Fast
- Robust in many situations
 - Particularly with N(L)PAR

- Cons:

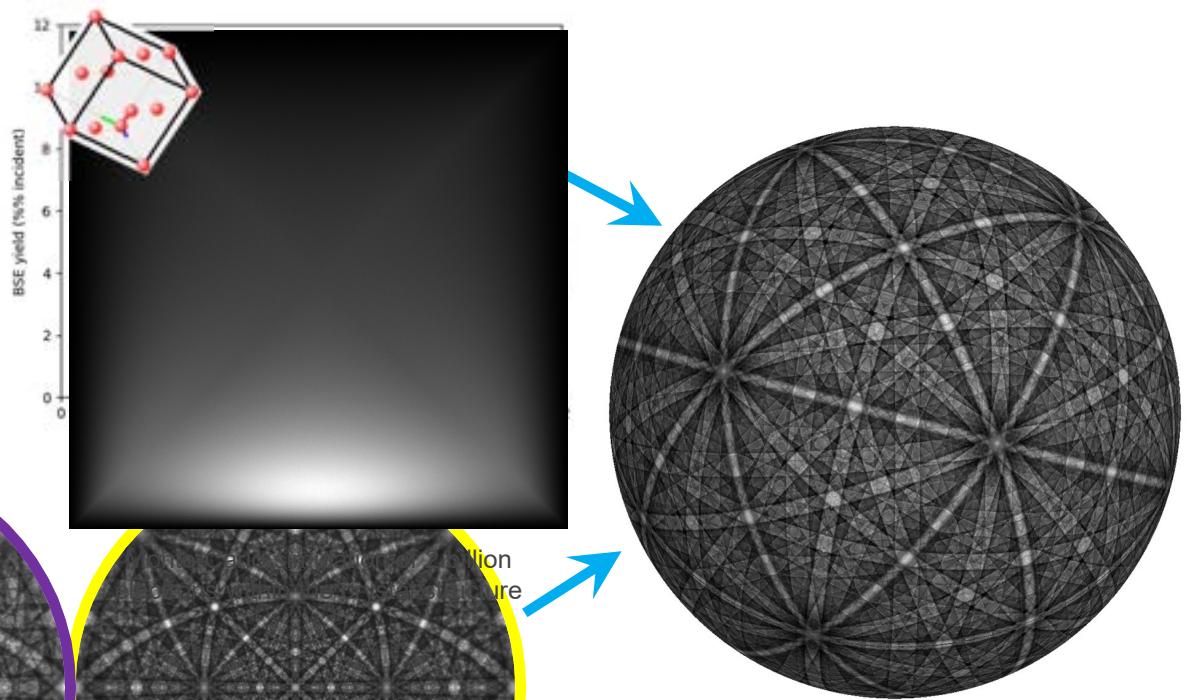
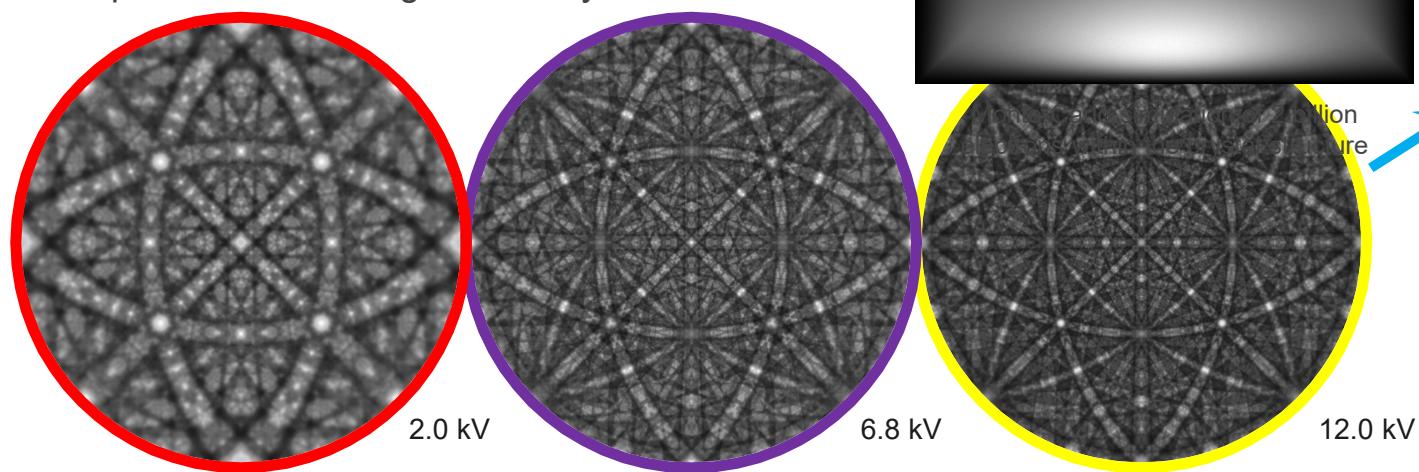
- Struggles with very poor patterns
- Determining the best reflectors can be a challenge for some crystals
- Angular resolution is $\sim 0.1^\circ - 0.5^\circ$ primarily dependent on pattern quality
- Difficulty resolving pseudosymmetry
- Unable to index non-centrosymmetric crystals (band intensity profiles vs band locations)



Can we improve on Hough
transform-based indexing?

Alternative indexing method: using dynamic pattern simulations

- Model the diffraction path of 2 billion electrons in a crystal using a Monte Carlo simulation for BSE yield
- Dynamical diffraction simulation is performed for each energy
- BSE weighted sum from all energies is combined into a single Kikuchi sphere
- Requires full knowledge of the crystal structure

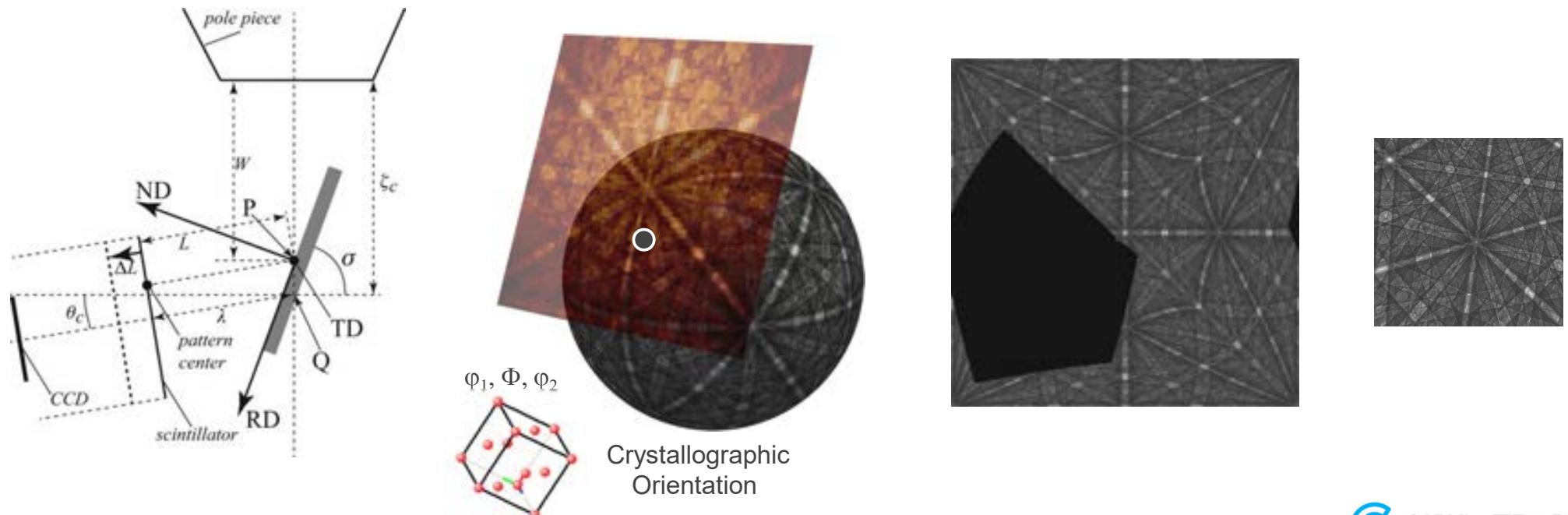


Callahan, P. G., & De Graef, M. (2013). Dynamical electron backscatter diffraction patterns. Part I: Pattern simulations. *Microscopy and Microanalysis*, 19(5), 1255-1265.

Dynamic pattern simulation

EBSD Pattern simulation

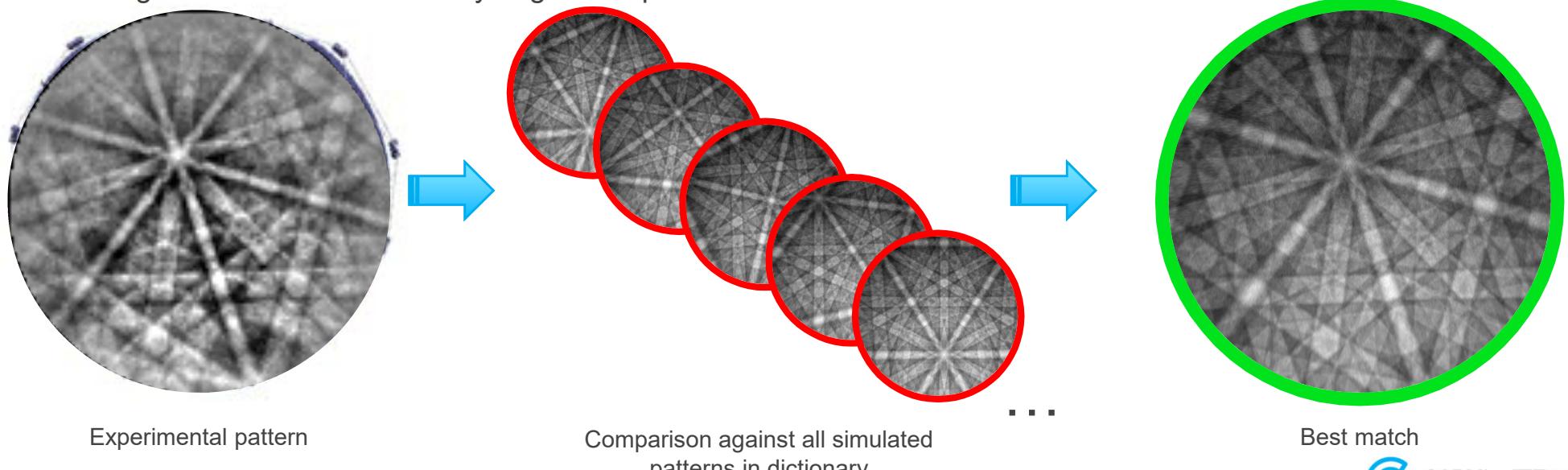
- Rotate Kikuchi sphere by orientation
- Project using the current calibration + crop to match the EBSD detector projection geometry



Callahan, P. G., & De Graef, M. (2013). Dynamical electron backscatter diffraction patterns. Part I: Pattern simulations. *Microscopy and Microanalysis*, 19(5), 1255-1265.

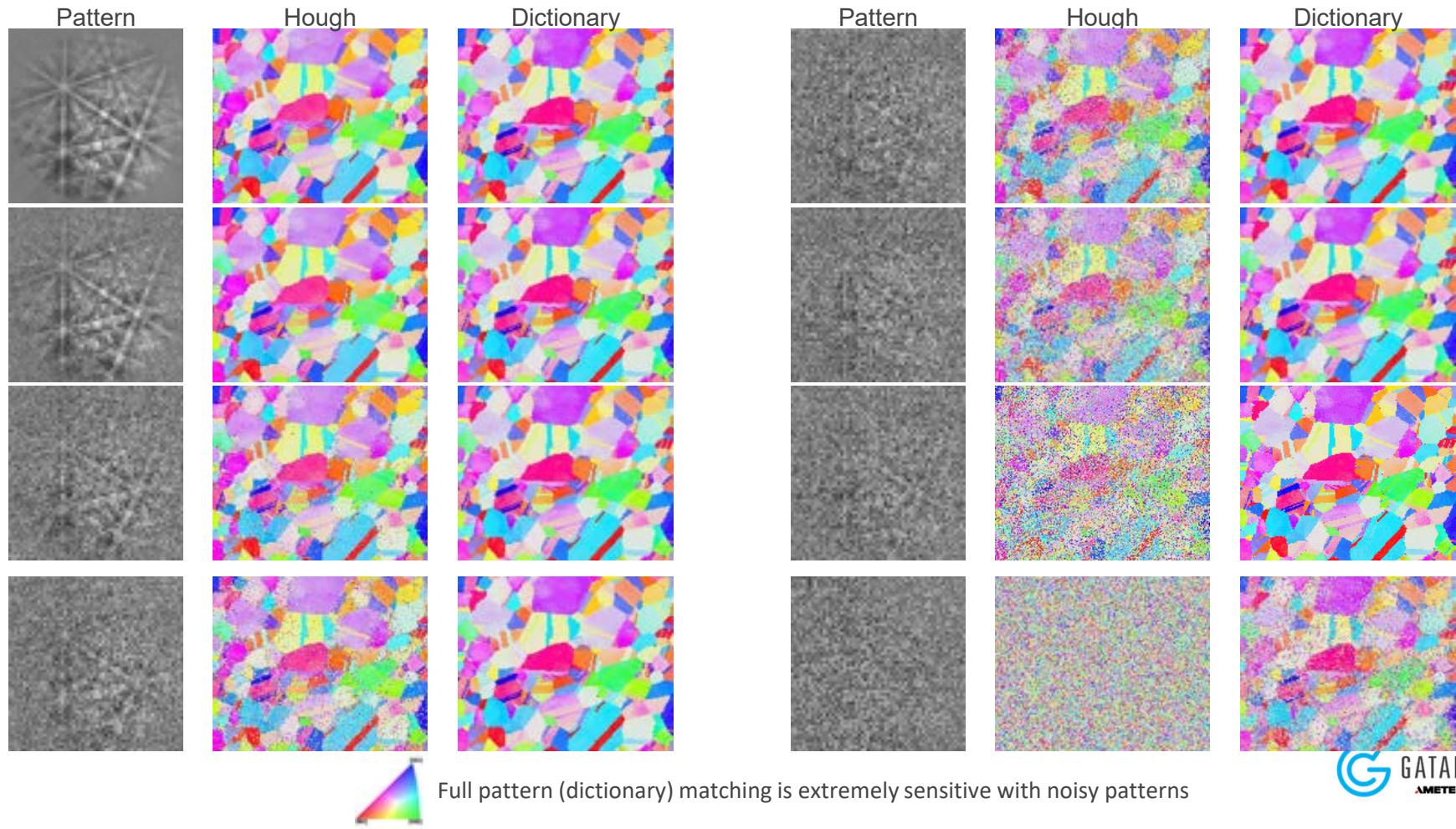
EBSD mapping using Dictionary Indexing – procedure

- Create a library (dictionary) of all patterns of all possible orientations on a predefined grid (e.g. every 2°)
- Compare each pattern in a scan against all patterns in the dictionary and find the best match
- Patterns in dictionary are created to match the actual pattern projection geometry in the SEM
 - Need to create a new library for each map/WD
- Matching success is determined by largest dot product of normalized column vectors



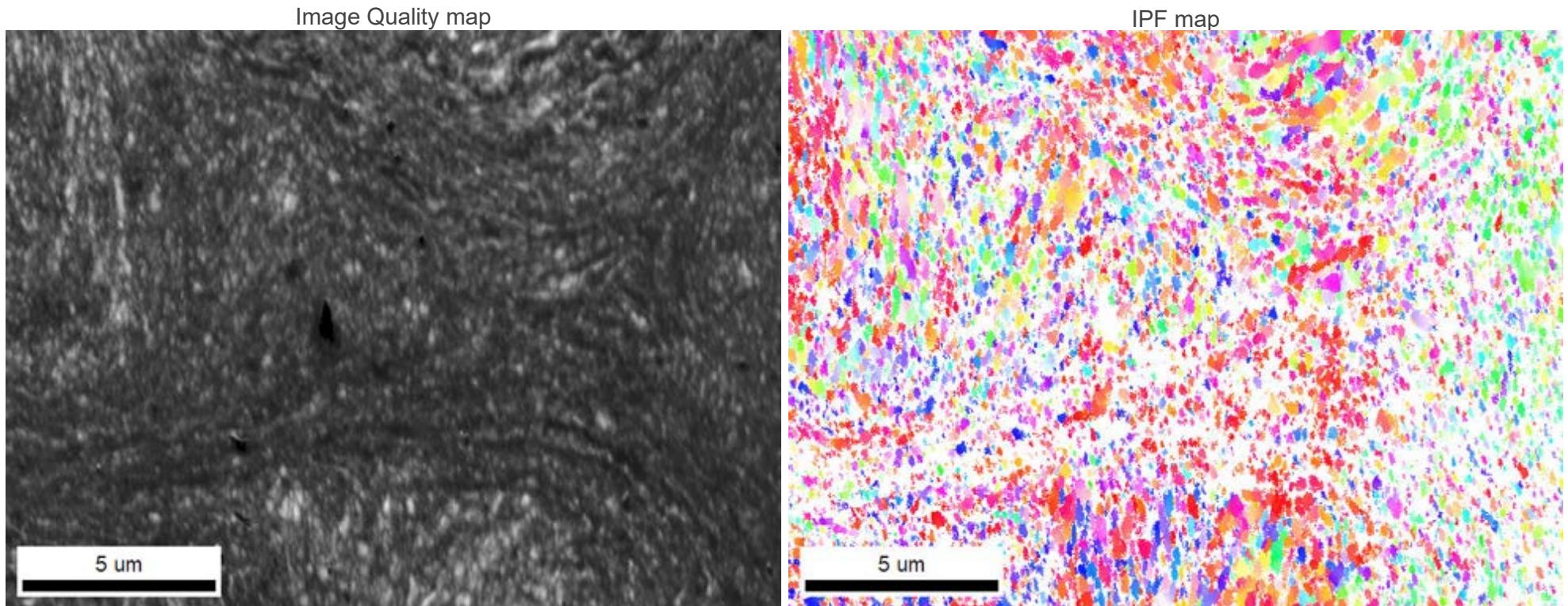
S. Singh and M. De Graef (2016). Orientation sampling for dictionary-based diffraction pattern indexing methods.
Modelling and Simulation in Materials Science and Engineering, **24**: 085013.

Dictionary indexing robustness - Nickel with varying noise



EBSD mapping using Dictionary Indexing – example

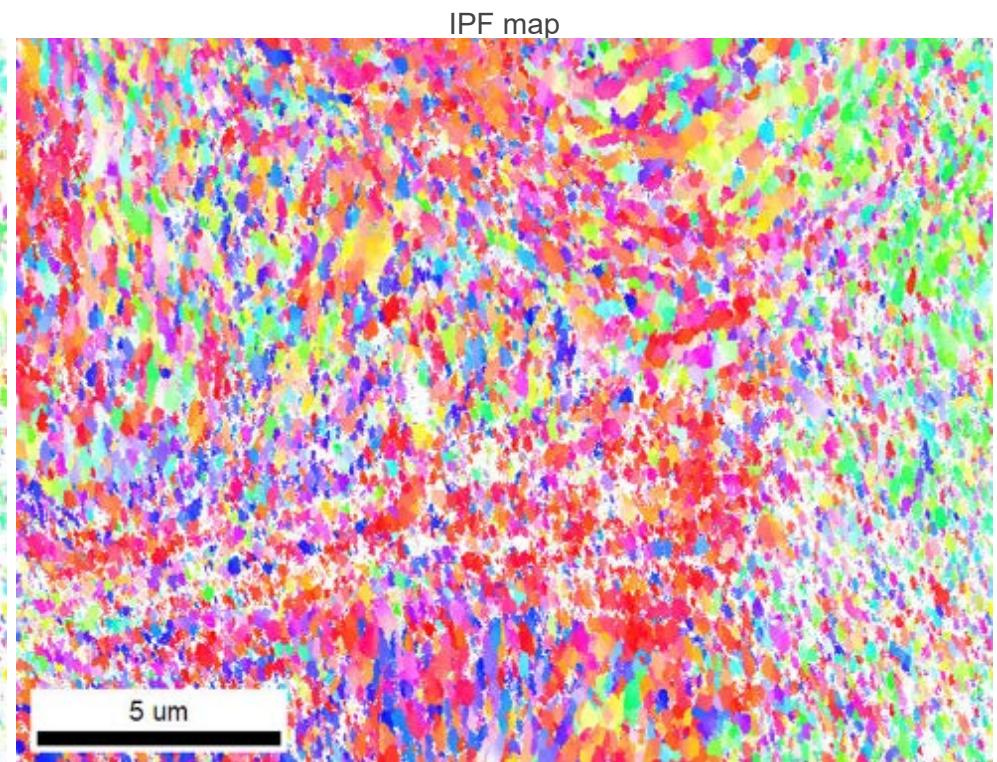
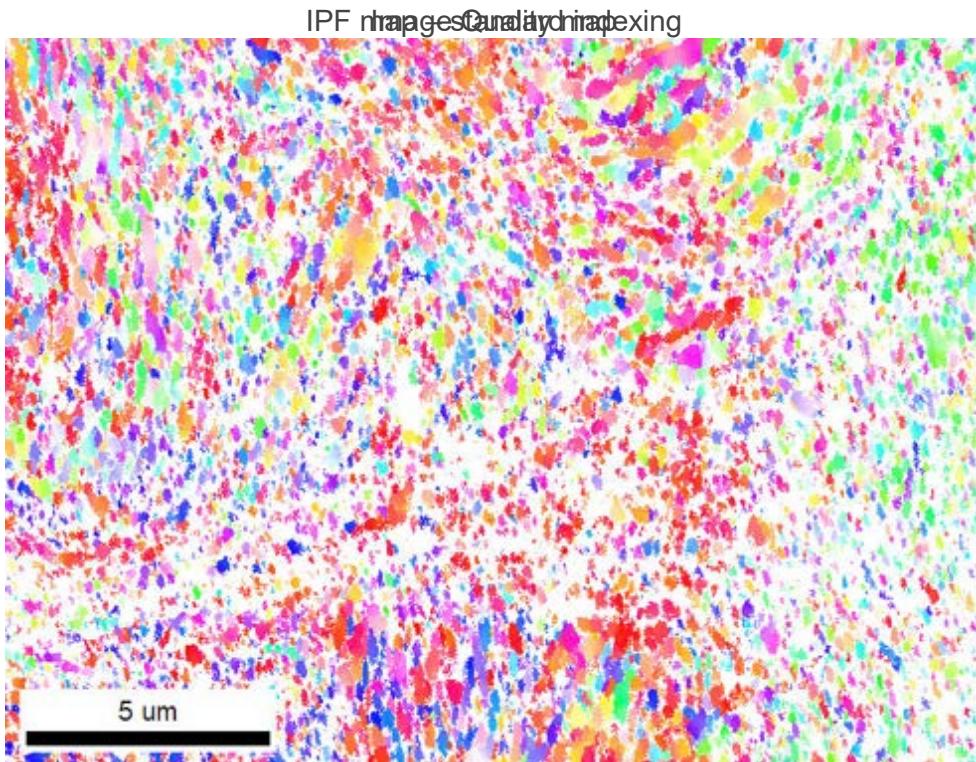
EBSD indexing improvements on highly deformed compressed ferrite powder sample



Hough indexing, ISR: 49.8%
Sample courtesy of Carsten Bonnekoh, KIT, Germany

EBSD mapping using Dictionary Indexing – example

EBSD indexing improvements on highly deformed compressed ferrite powder sample



Dictionary indexing, ISR: 82.3%
Sample courtesy of Carsten Bonnekoh, KIT, Germany

 GATAN +  EDAX
AMETEK

Dictionary indexing – Pros & cons

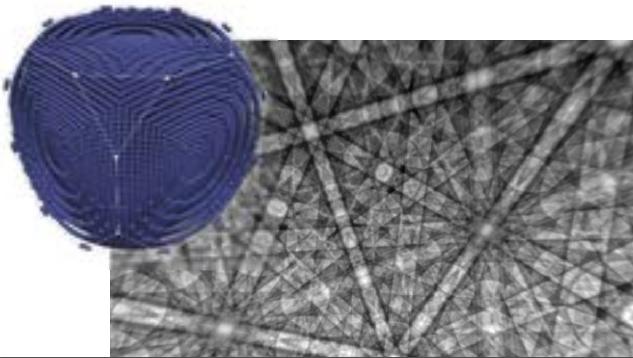
- More robust than Hough indexing
- Significantly slower than Hough indexing
 - Large dictionaries (particularly for low symmetries)
 - Angular resolution
- Steep learning curve
 - Master pattern calculation
 - Dictionary spacing
 - Refinement parameters

Singh, S., Ram, F., & De Graef, M. (2017). EMsoft: open-source software for electron diffraction/image simulations. *Microscopy and Microanalysis*, 23(S1), 212-213.

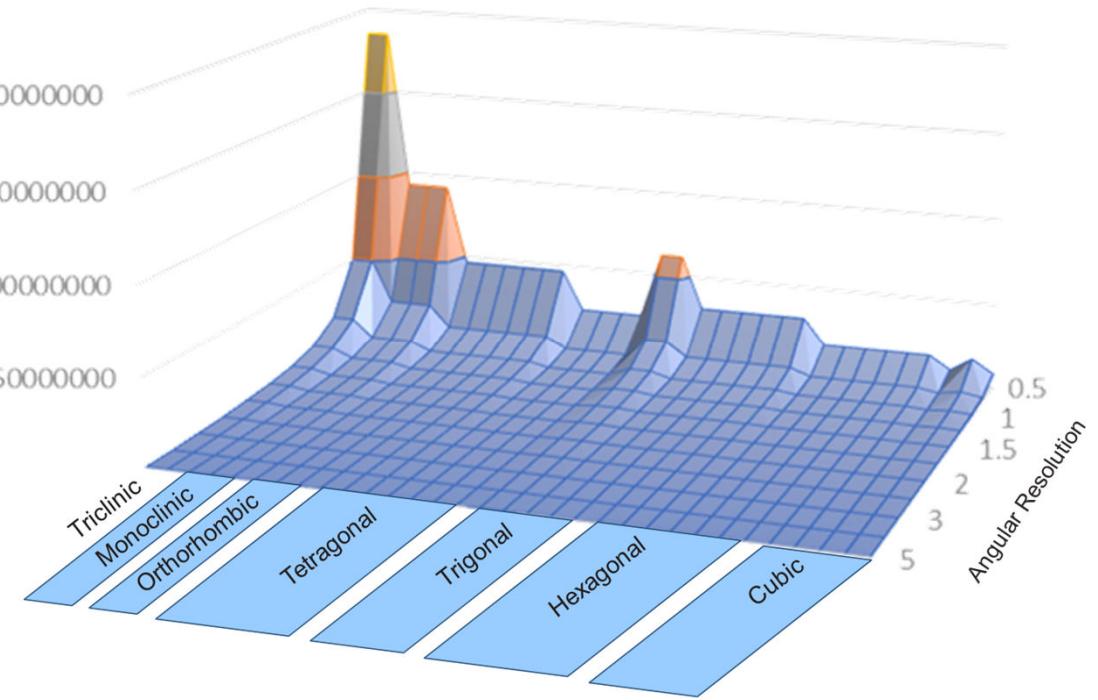
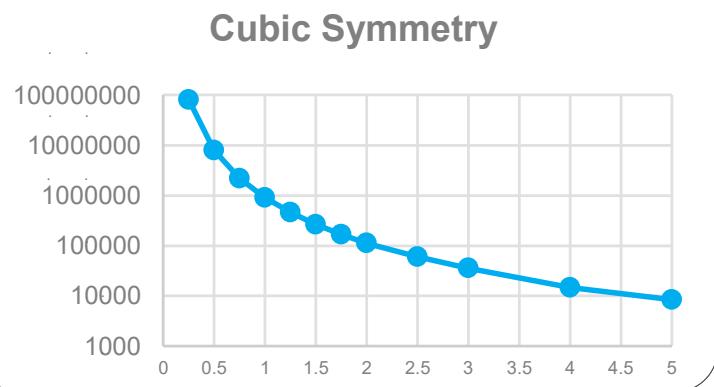


Dictionary indexing limitation – dictionary size

- Dictionary size is related to crystal symmetry and initial grid resolution

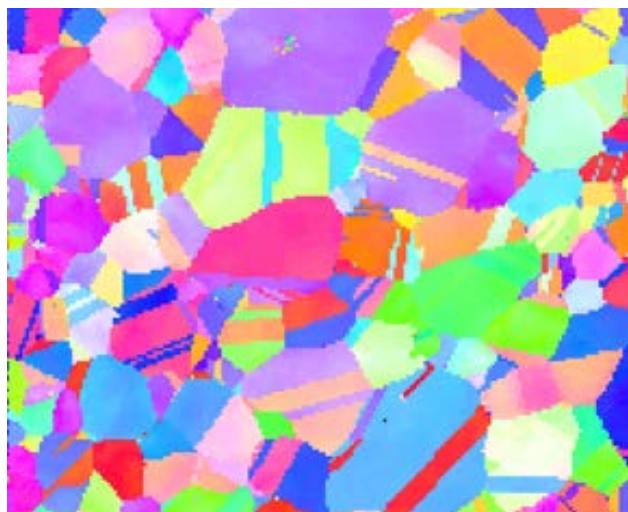


Patterns

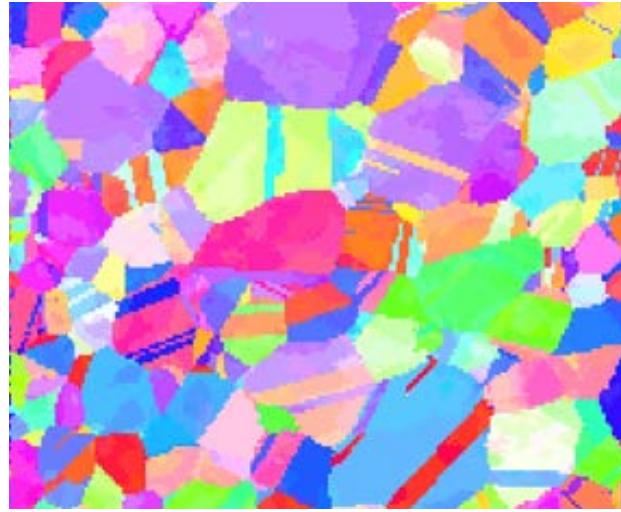


Minimum dictionary spacing

Hough-based



2.5° Dictionary



5° Dictionary



Minimum spacing is not just about angular precision but also indexing reliability

2D dictionary indexing

Known 'full' scene



Create a dictionary of patterns to match the detector size



Detected image
(includes noise)



Find the best match against the dictionary to locate where the detected image falls within the full scene



Alan Fink "Portland Head Light," Kodak Image 21 (SP91052)

 GATAN +  EDAX
AMETEK

Alternative: 2D cross-correlation – Fourier transform

Known 'full' scene



$f(x)$

Detected
image
(includes
noise)



$g(x)$

Calculate cross-correlation



$$\mathcal{F}^{-1} \left\{ \overline{\mathcal{F}\{f\}} \mathcal{F}\{g\} \right\}$$

\mathcal{F}

Fourier transform

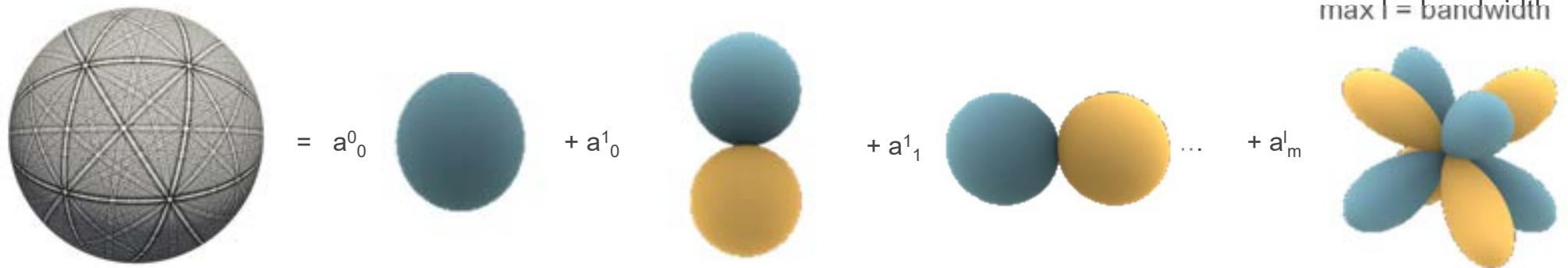
Use Cross-Correlation peak to
locate detected image within scene



Alan Fink "Portland Head Light," Kodak Image 21 (SP91052)

 GATAN +  EDAX
AMETEK

Spherical harmonic transform



Fourier transform

Forward

\mathcal{F}

$$\hat{f}_m^l \triangleq \mathcal{S}\{f(\theta, \phi)\} = \int_{\theta=0}^{\pi} \int_{\phi=0}^{2\pi} f(\theta, \phi) \overline{Y_m^l(\theta, \phi)} \sin \theta d\phi d\theta$$

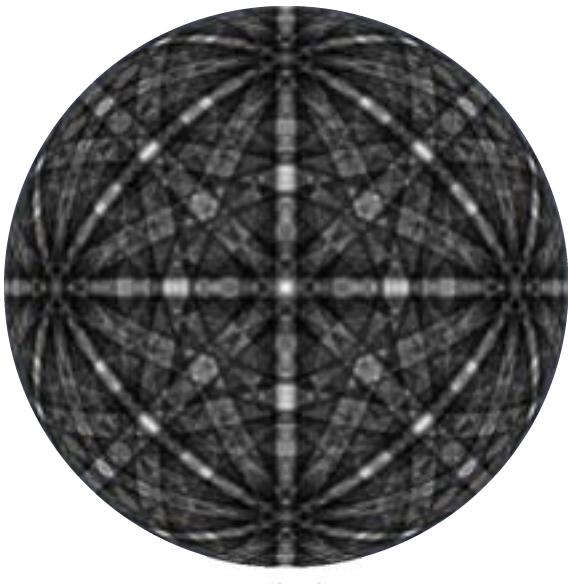
Inverse

\mathcal{F}^{-1}

$$f(\theta, \phi) = \sum_{m=-l_{max}}^{l_{max}} \sum_{l=|m|}^{l_{max}} \hat{f}_m^l Y_m^l(\theta, \phi)$$

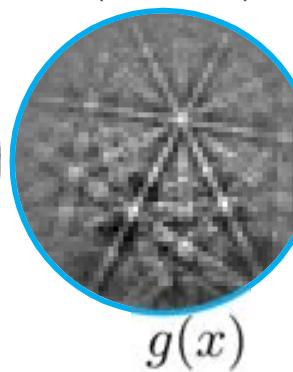
Can we do cross-correlation on a sphere?

Full Scene: Simulated master
Pattern of diffraction on a sphere



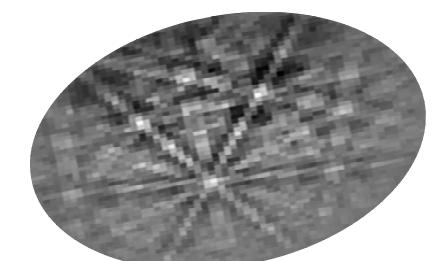
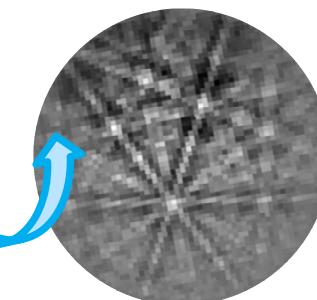
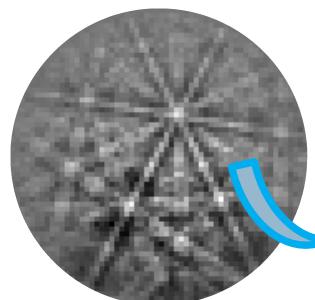
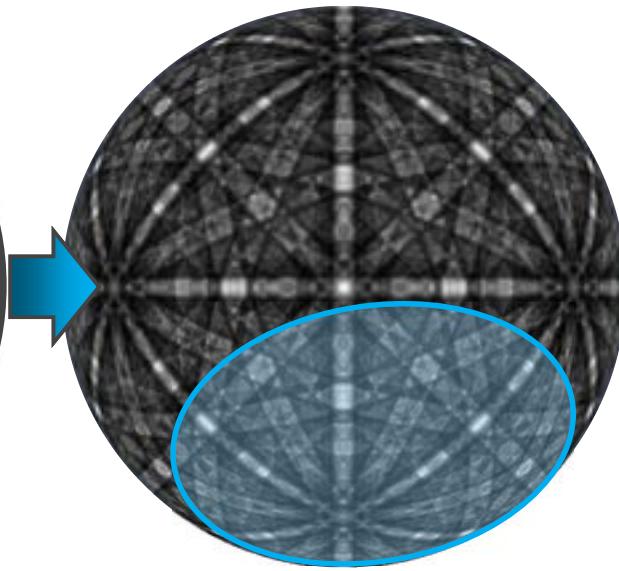
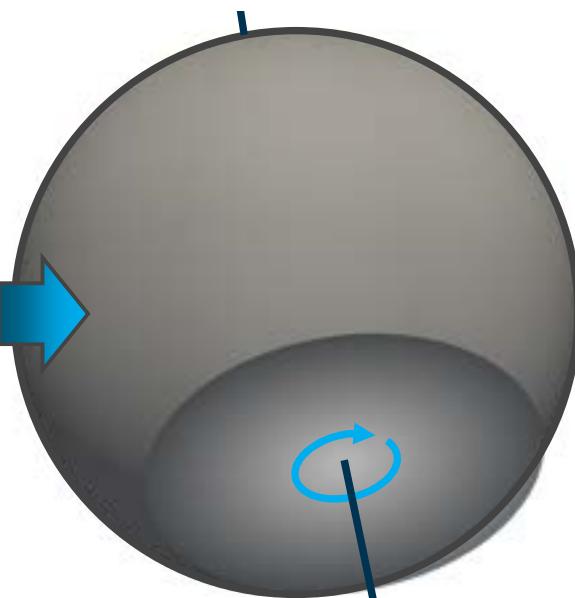
$f(x)$

Detector pattern
(corrected)



$g(x)$

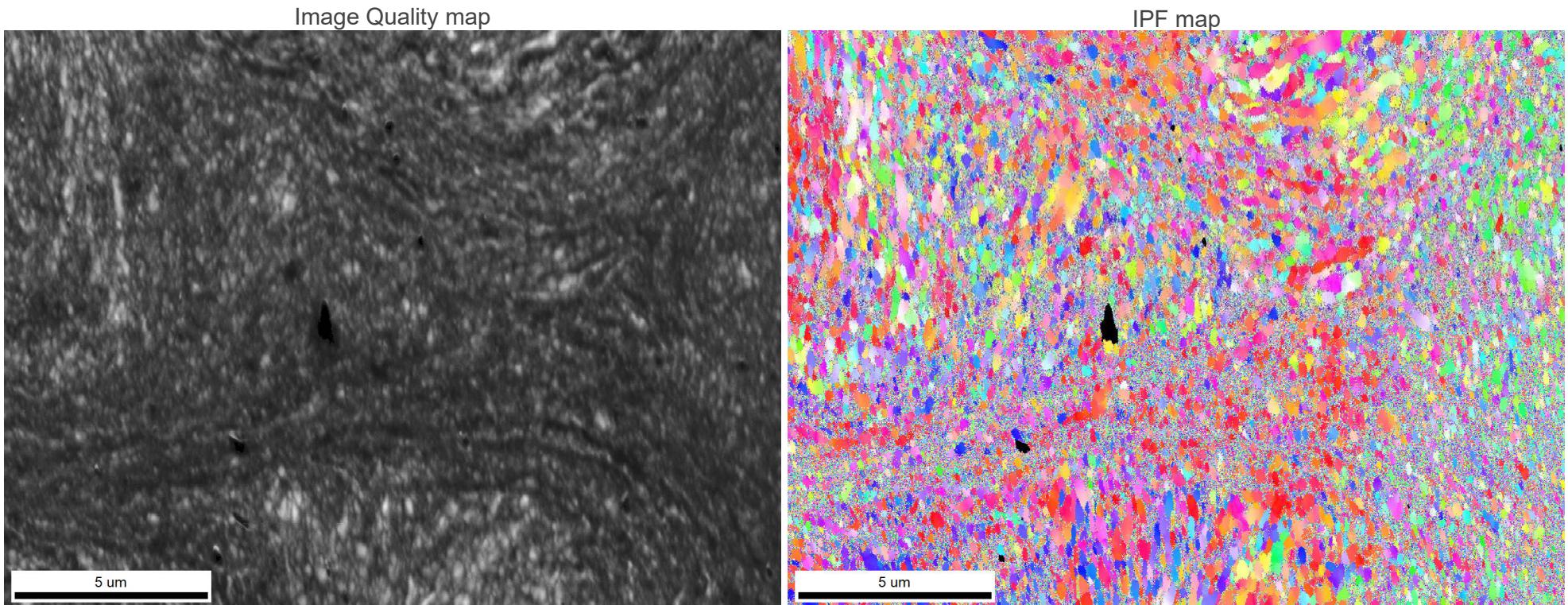
Cross-correlation on the sphere



Note: this analog to the 2D lighthouse example is oversimplified. One difference of 3D spherical problem relative to the 2D planar example is the rotational component.

EBSD mapping using Hough-based indexing

EBSD indexing improvements on highly deformed compressed ferrite powder sample



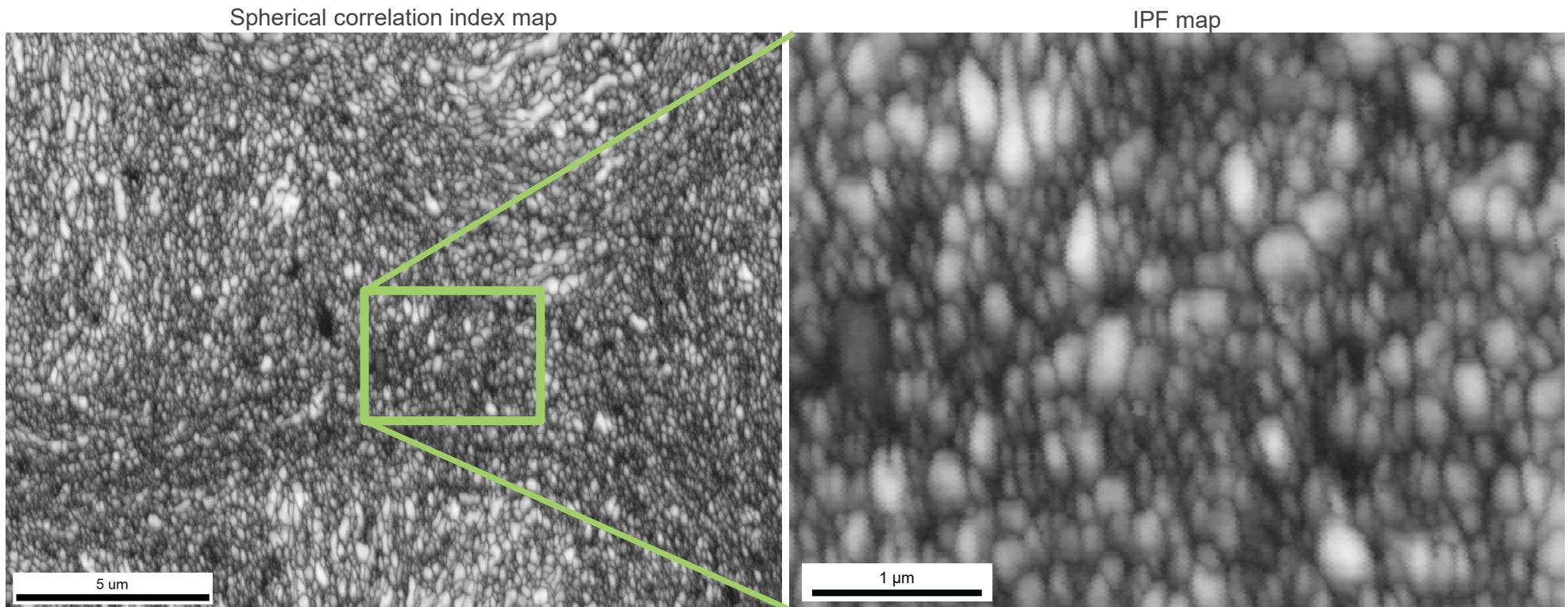
Hough indexing

Sample courtesy of Carsten Bonnekoh, KIT, Germany

 GATAN +  EDAX
AMETEK

EBSD mapping using Spherical indexing with NPAR

EBSD indexing improvements on highly deformed compressed ferrite powder sample

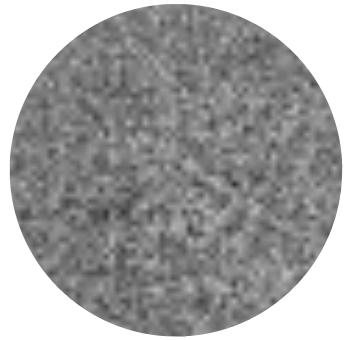


Hough indexing, ISR: 98.1%
Sample courtesy of Carsten Bonnekoh, KIT, Germany

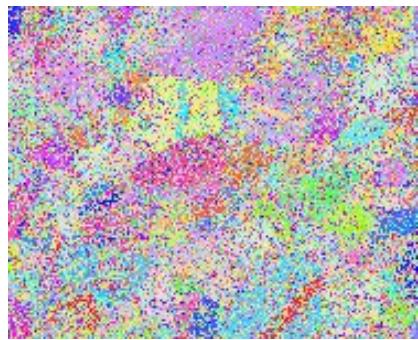
 GATAN +  EDAX
AMETEK

Spherical EBSD indexing robustness

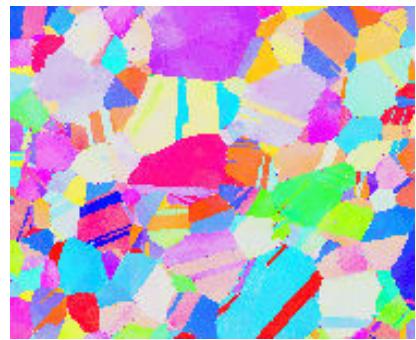
First Pattern



Hough Indexing
(NPAR)



Dictionary Indexing
(2.5°)



Bandwidth = 53



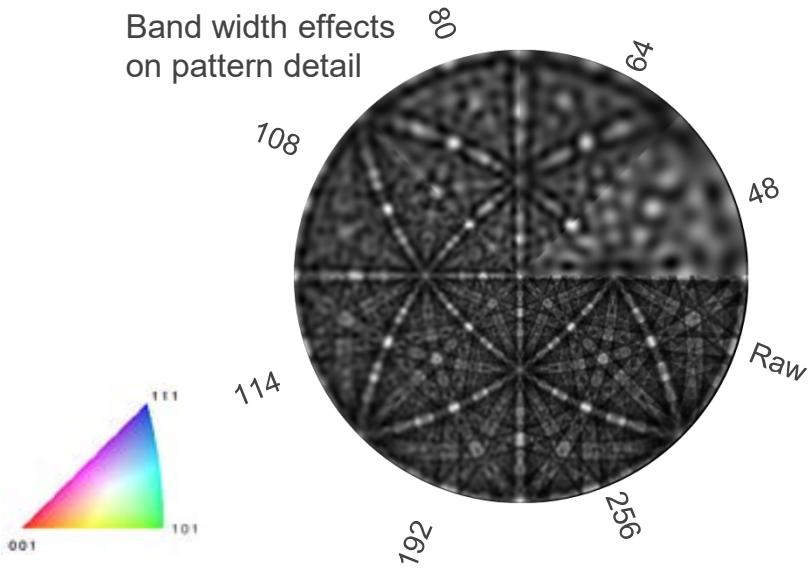
Bandwidth = 63



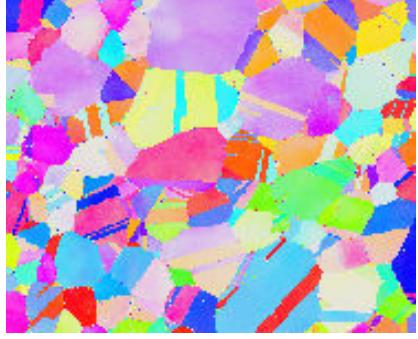
Bandwidth = 74



Band width effects
on pattern detail



Bandwidth = 88

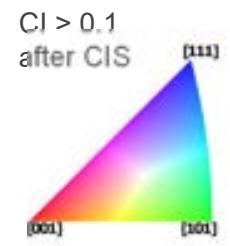
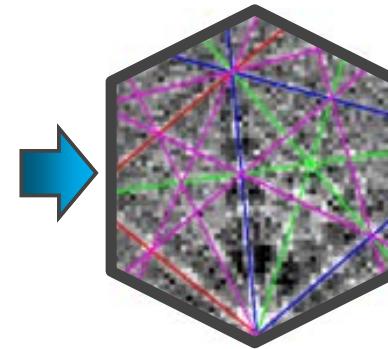
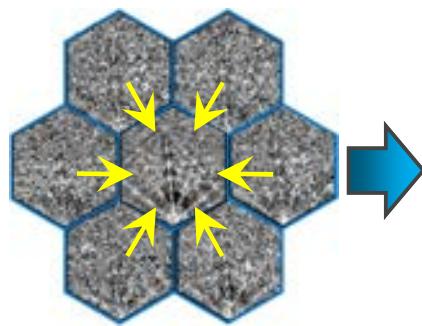
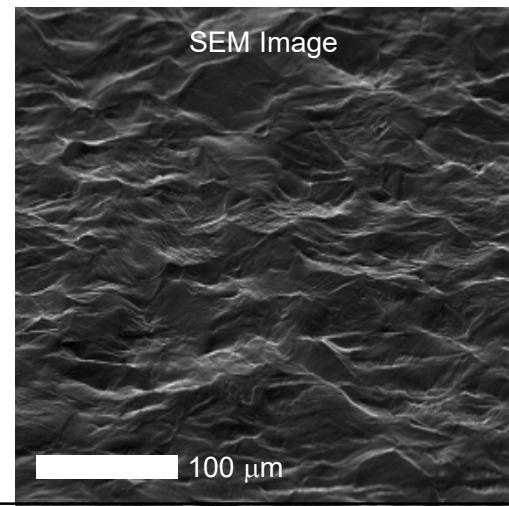
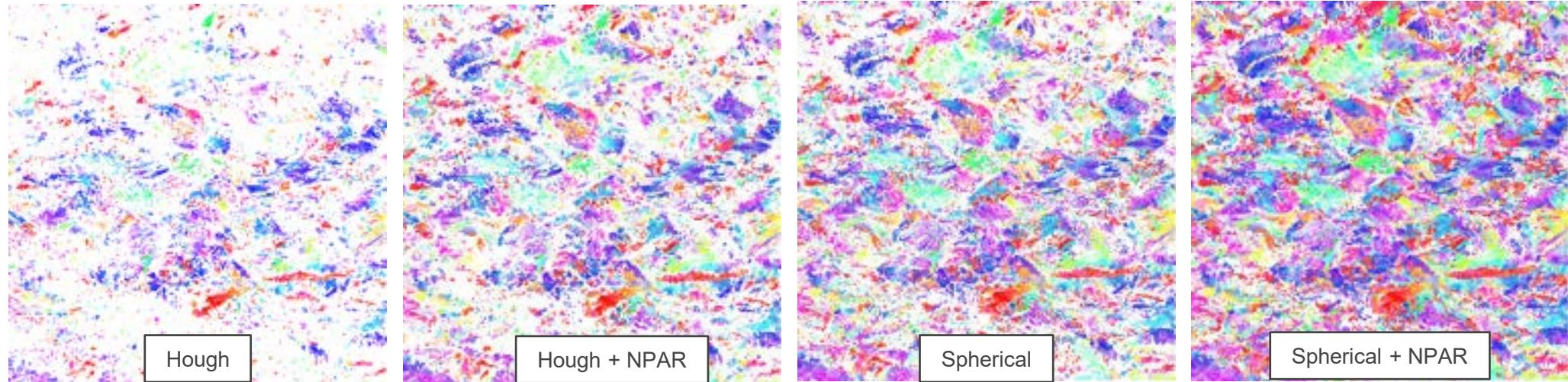


Bandwidth = 113



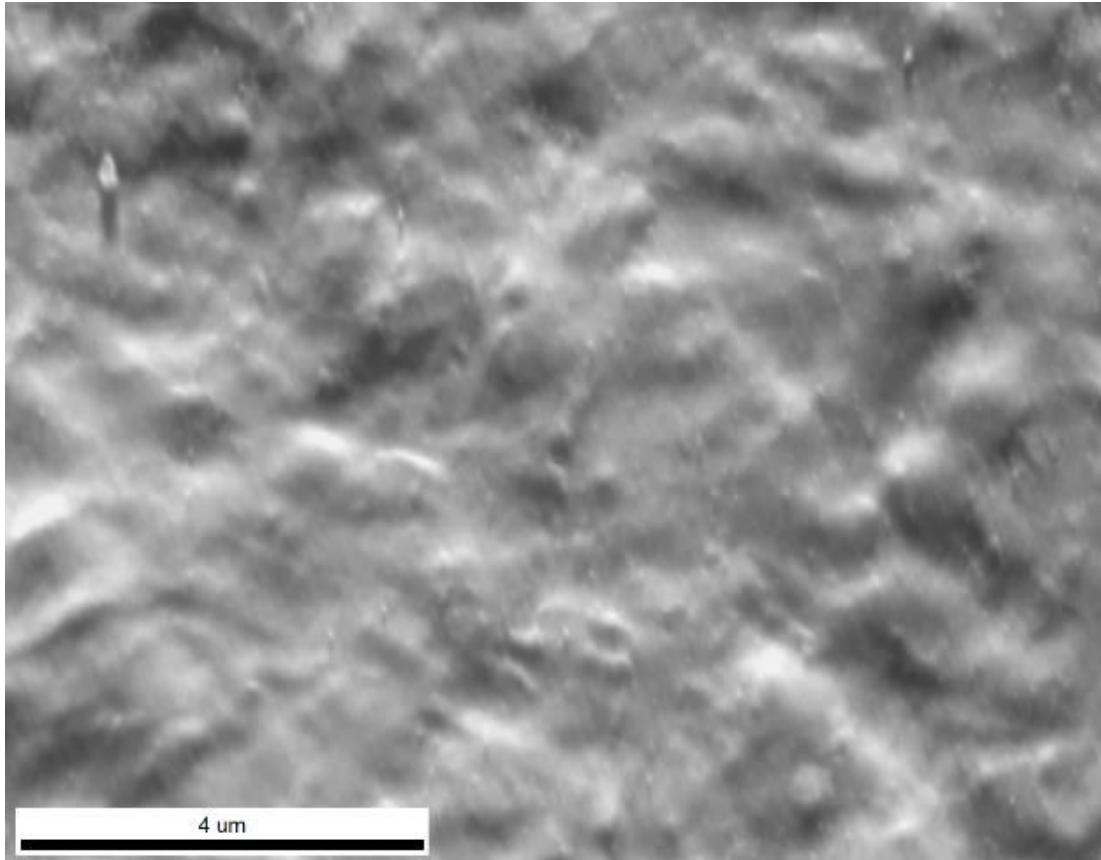
Lenthe, W. C., Singh, S., & De Graef, M. (2019). A spherical harmonic transform approach to the indexing of electron back-scattered diffraction patterns. *Ultramicroscopy*, 207, 112841.

Tensile sample – rough surface



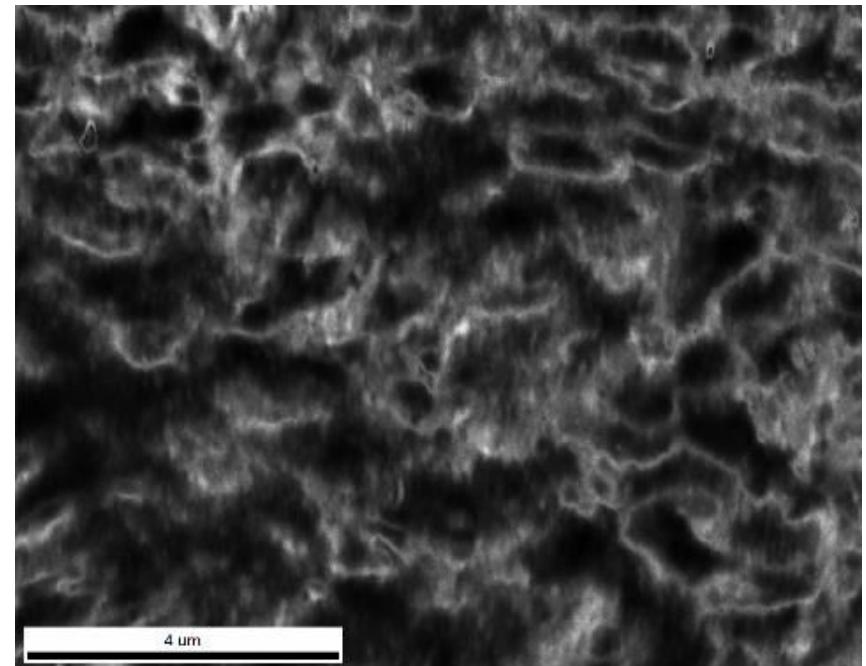
Brewick, P.T., Wright, S.I. & Rowenhorst D.J. (2019). NLPAR: Non-local smoothing for enhanced EBSD pattern indexing. *Ultramicroscopy*, 200, 50-61.

Titanium nitride coating with sub-micron grain size



SEM image of analysis area

- TiN coating on coarse grained polycrystalline substrate – rough surface
- No additional surface preparation for EBSD



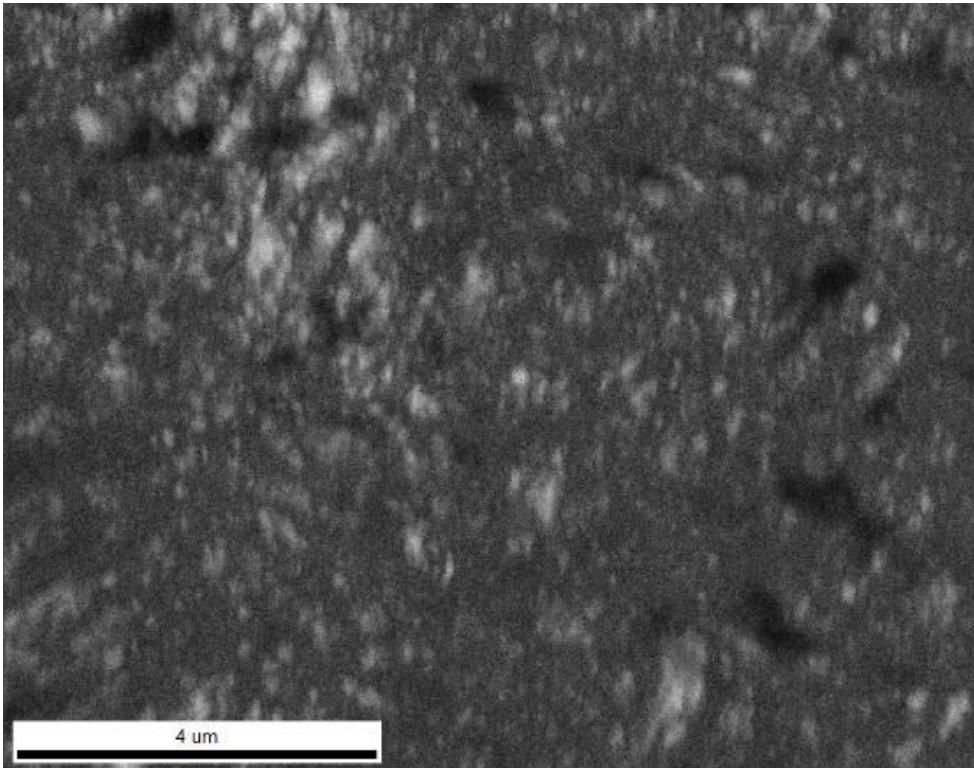
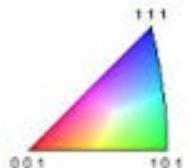
IQ map as measured

 GATAN +  EDAX
AMETEK

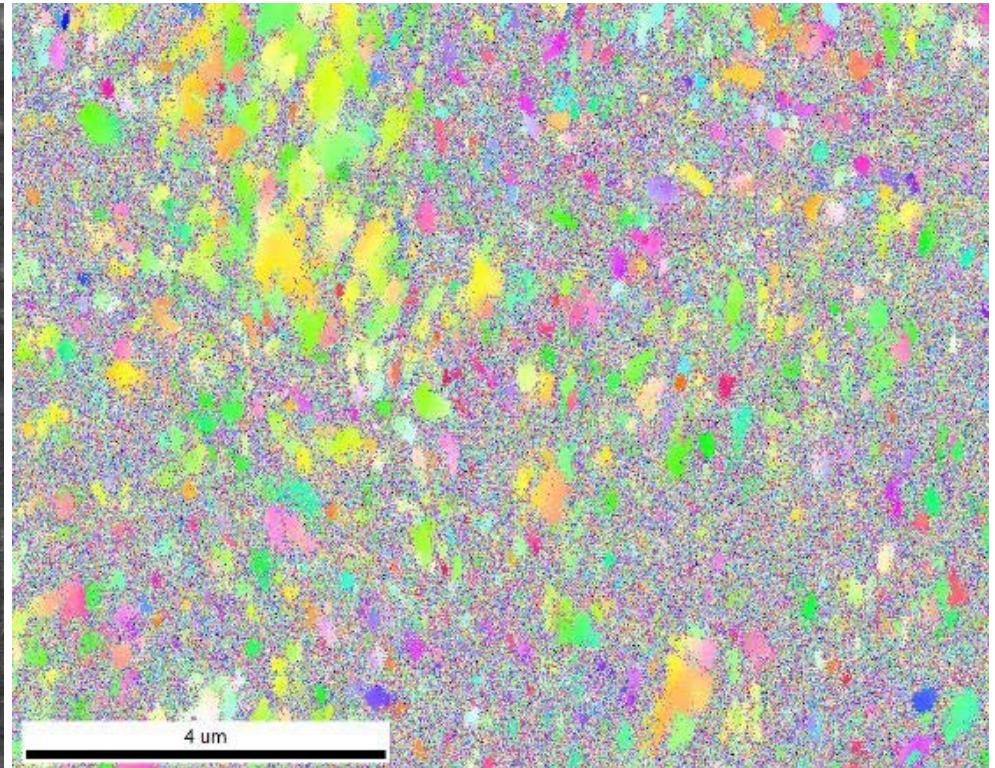
480,217 points, 10.89 x 8.57 μ m, 15 nm steps

Titanium nitride coating – Hough results

- Weak patterns combined with strong overlap at boundaries prevents successful indexing

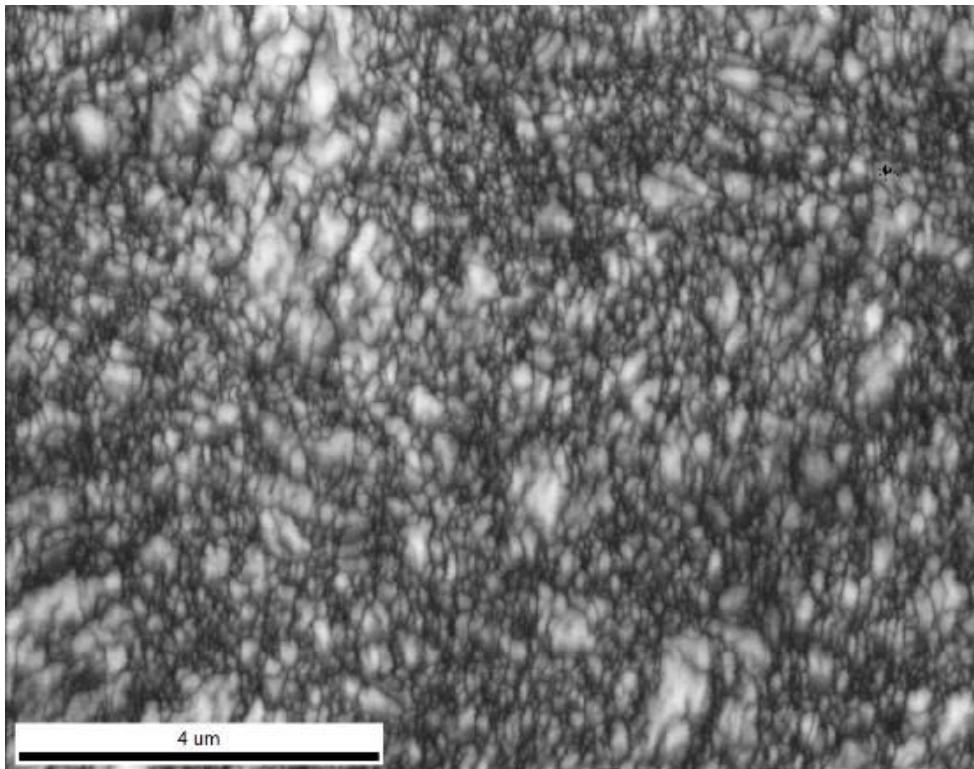


IQ map after pattern intensity homogenization

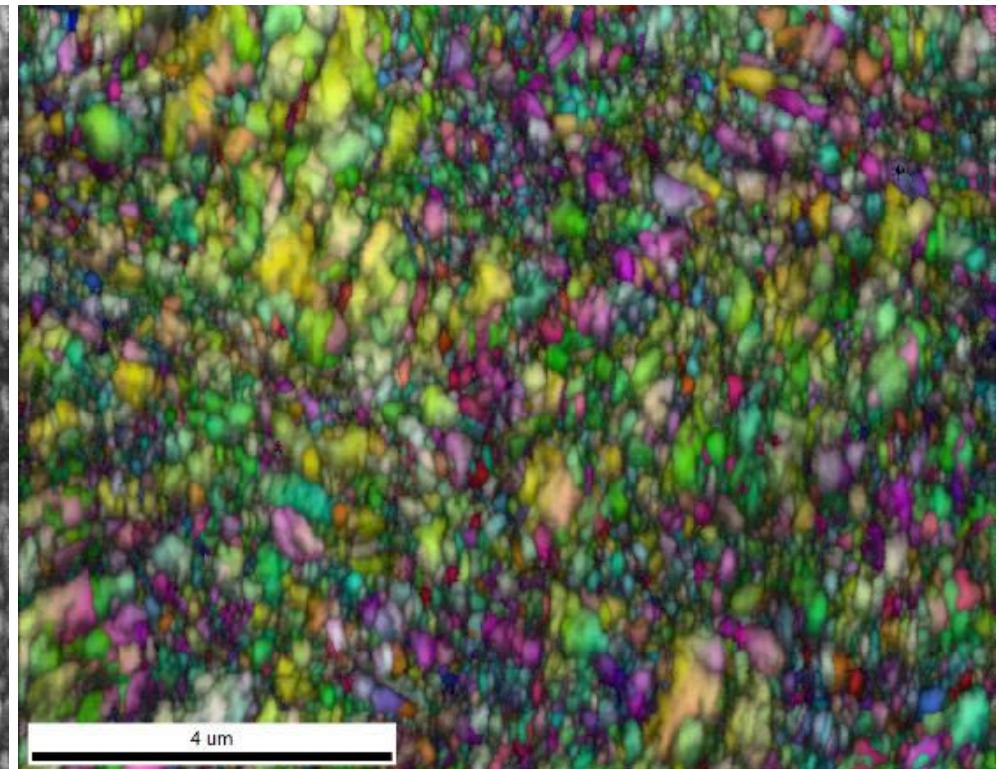


Titanium nitride coating – Spherical indexing results

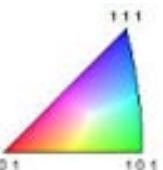
- Indexing results with spherical indexing



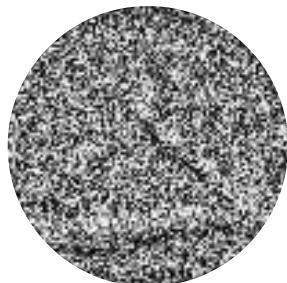
Spherical correlation map



IPF map – indexing success: 96% 



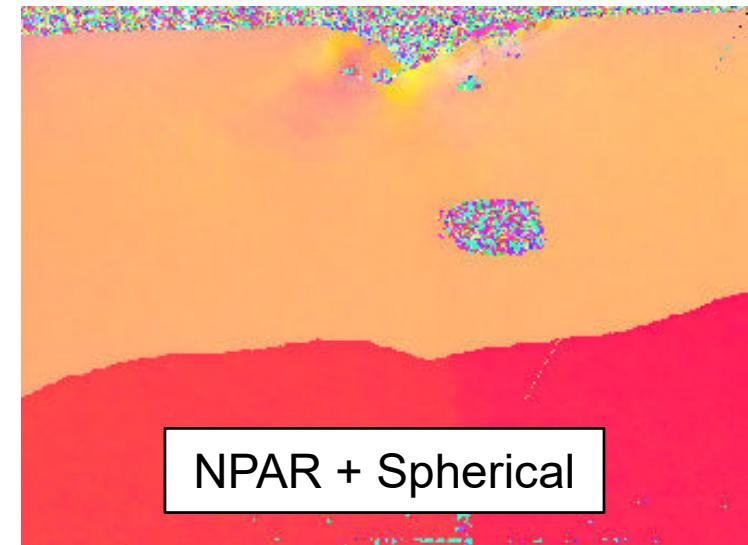
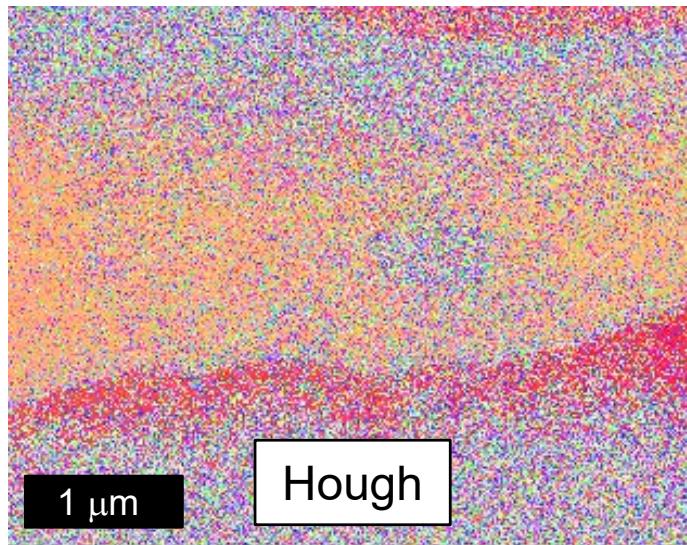
TKD - ferrite



AHE

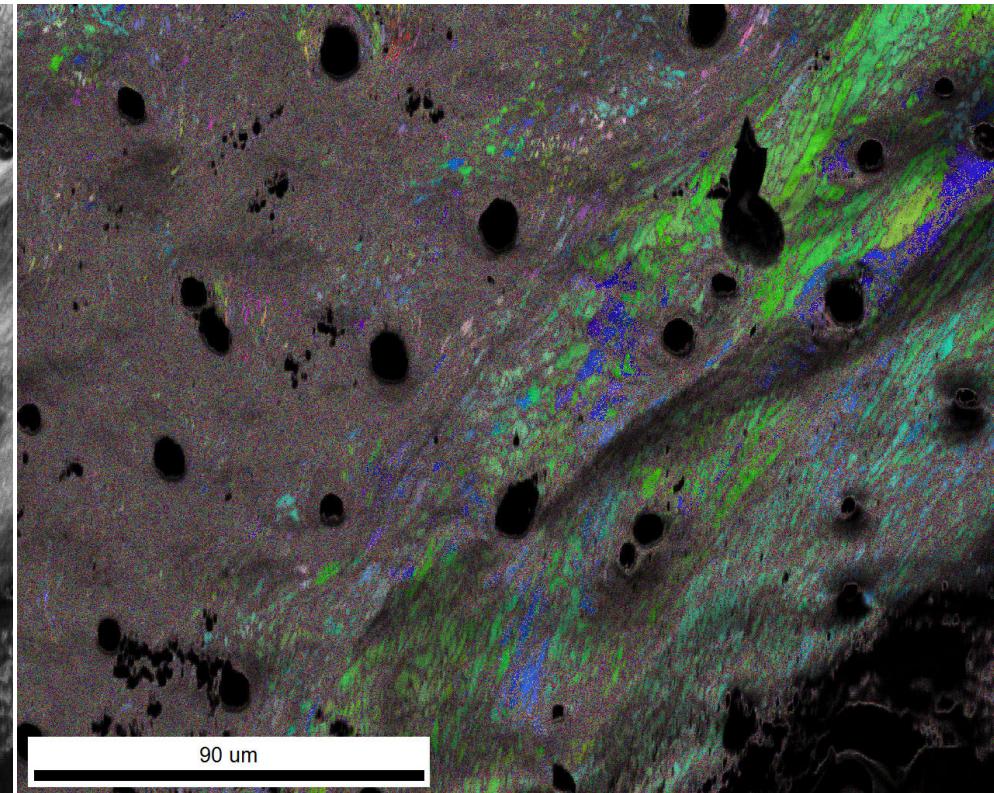
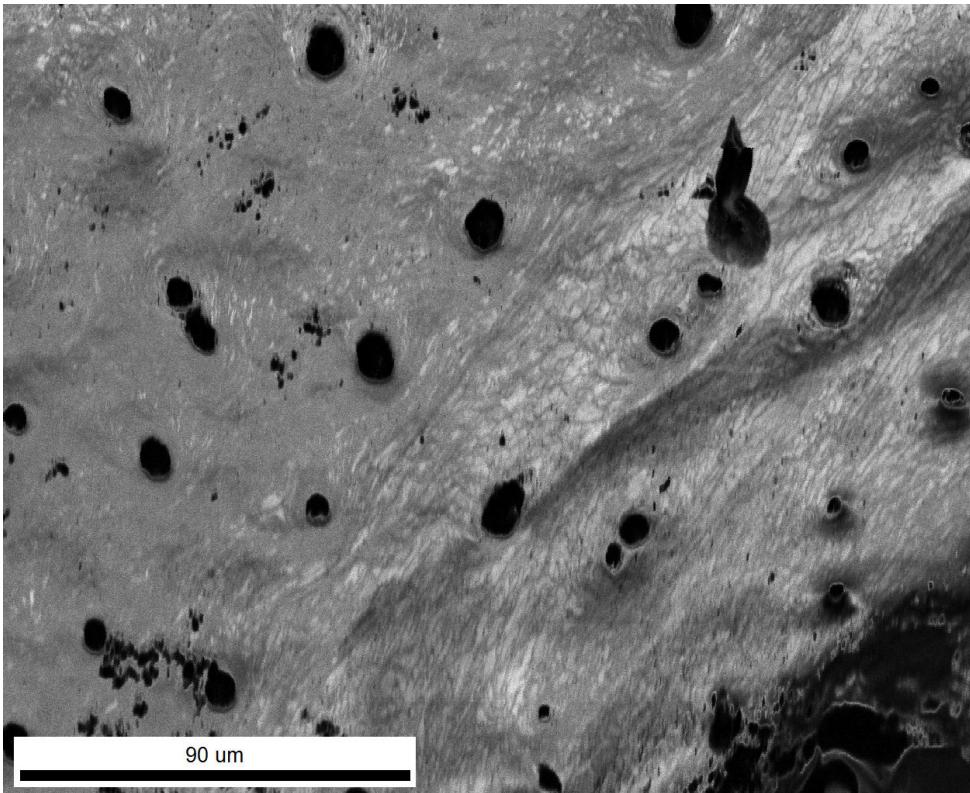


NPAR



- TKD samples often show significant gradients in pattern quality and intensity due to thickness variations
 - Image processing using AHE (adaptive histogram equalization) allows consistent matching with the master patterns
- Band width may change strongly within patterns due to the projection geometry
- Spherical indexing can help overcome these challenges

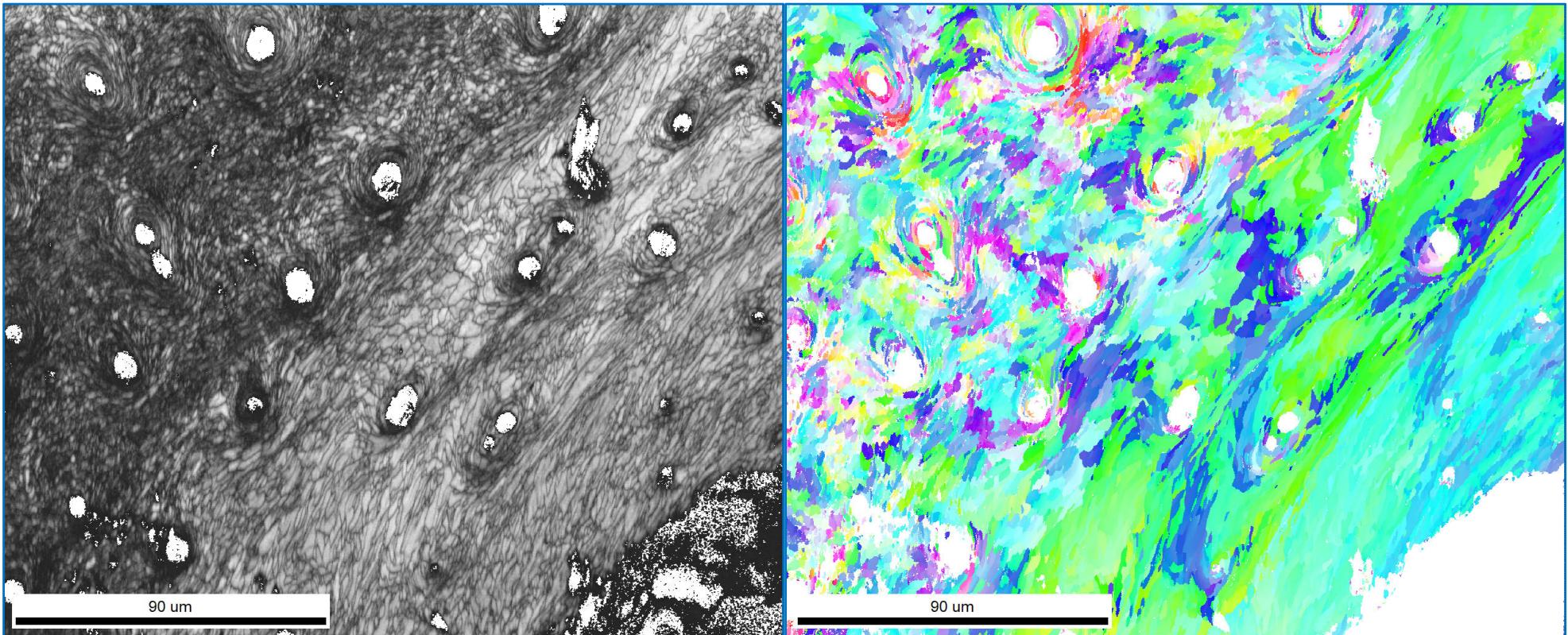
Beam sensitive bio-mineral example: brachiopod cross-section



Specimen courtesy of E. Griesshaber, Geo- und Umweltwissenschaften, Ludwig-Maximilians-Universität München

 GATAN +  EDAX
AMETEK

Brachiopod shell – spherical indexing

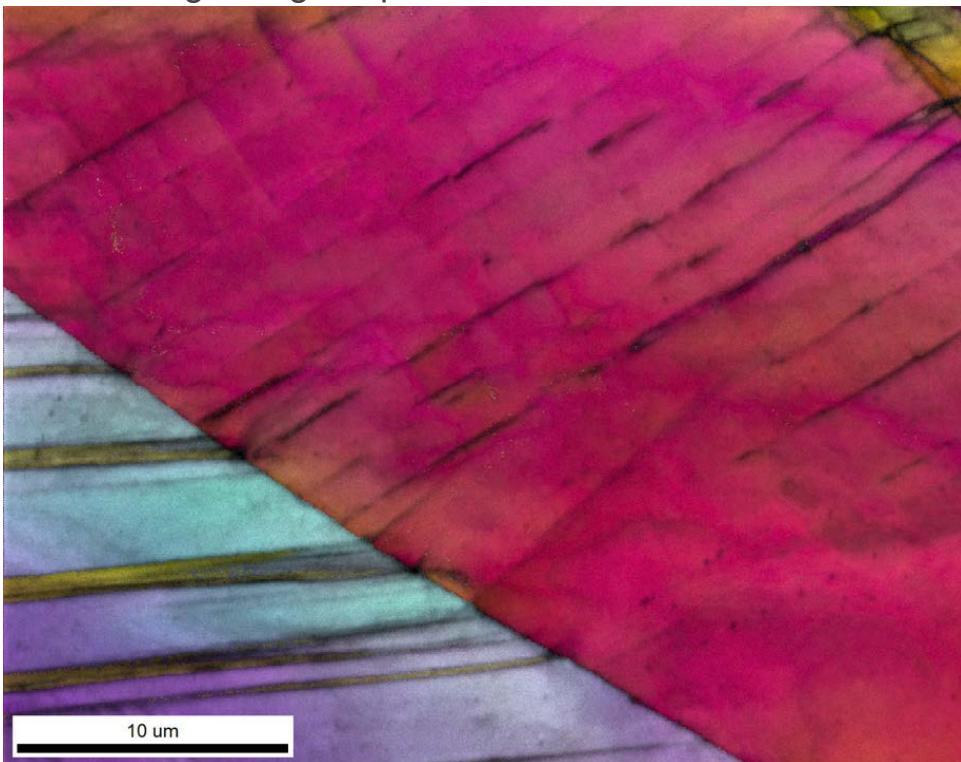


Specimen courtesy of E. Griesshaber, Geo- und Umweltwissenschaften, Ludwig-Maximilians-Universität München

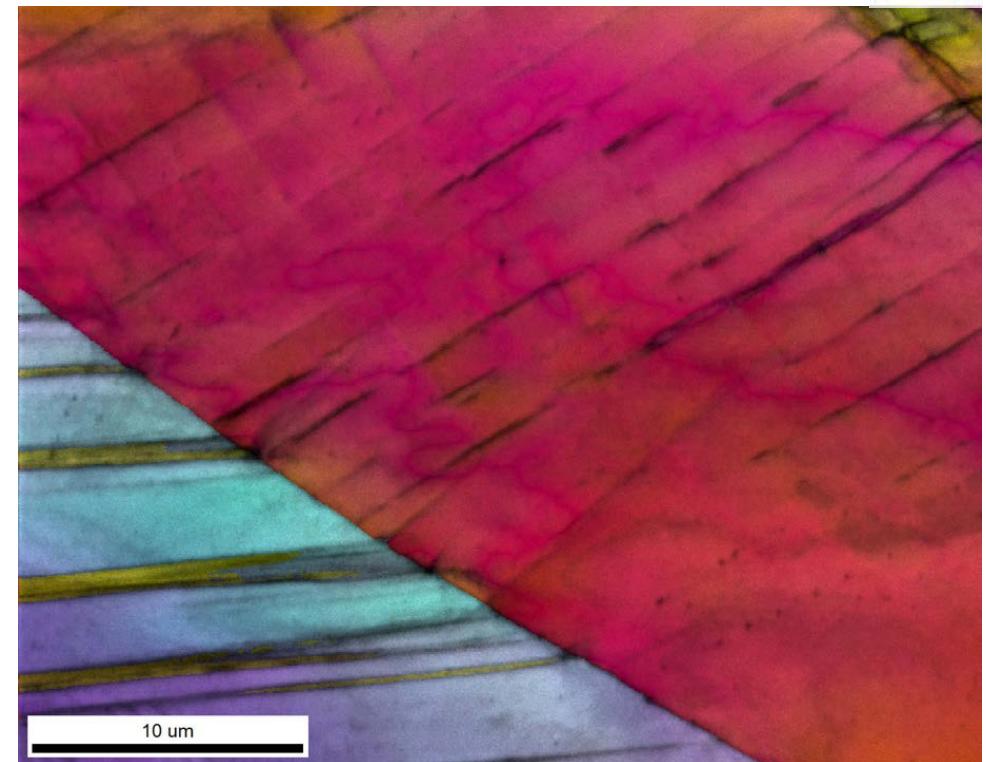
 GATAN +  EDAX
AMETEK

Spherical indexing – orientation precision improvements

- Because spherical indexing uses the entire pattern, you can get greatly improved orientation precision when working with good patterns



Triplet voting indexing

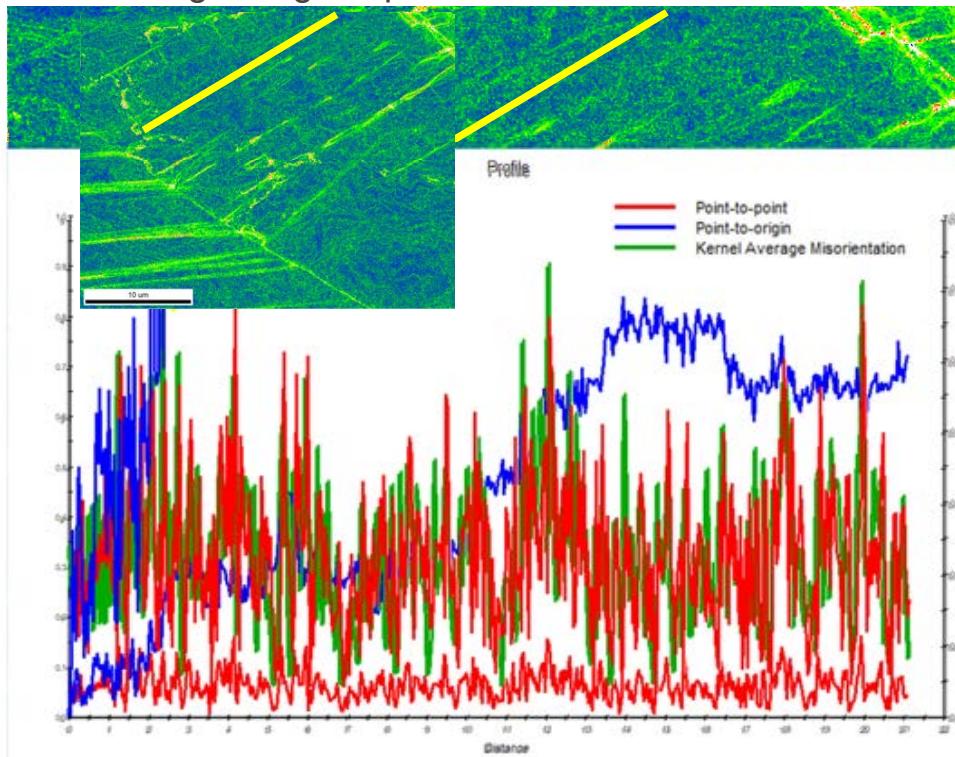


Spherical indexing

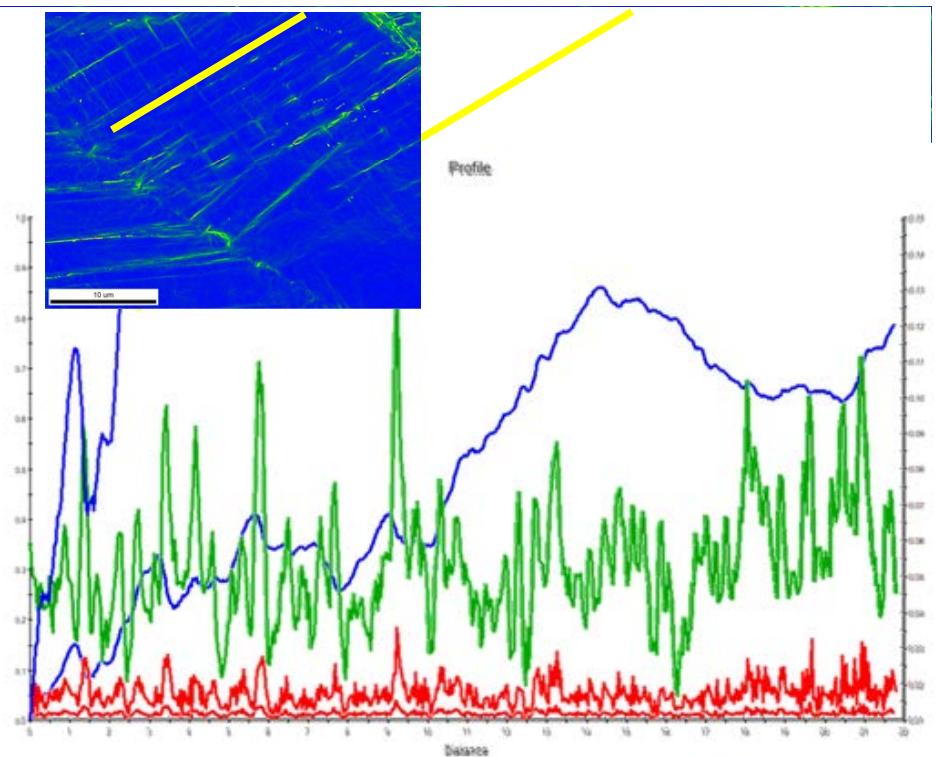


Spherical indexing – orientation precision improvements

- Because spherical indexing uses the entire pattern, you can get greatly improved orientation precision when working with good patterns



Kernel Average Misorientation 0.00 2.00
Triplet voting indexing



Precision better than 0.05°

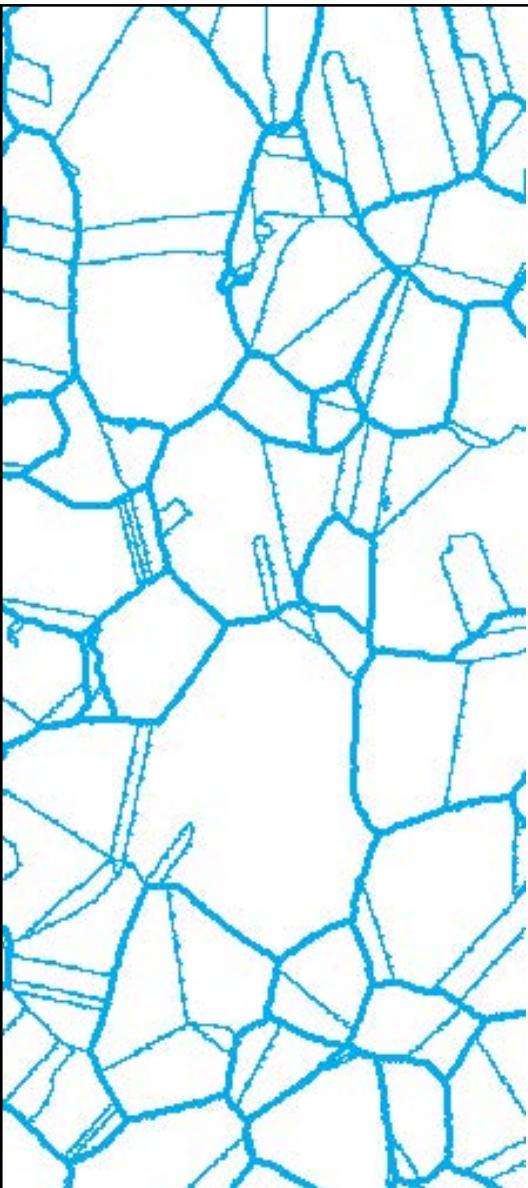
Spherical indexing

Summary

Spherical Indexing

- + As robust as Dictionary Indexing but faster
- + Higher angular precision than Hough
- + No pre-calculation of a dictionary required
- Slower than Hough
- Master Pattern required
- Image Processing: Adaptive Histogram Equalization

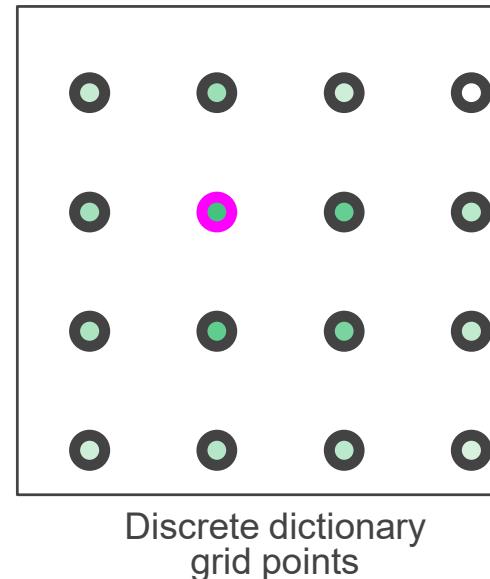
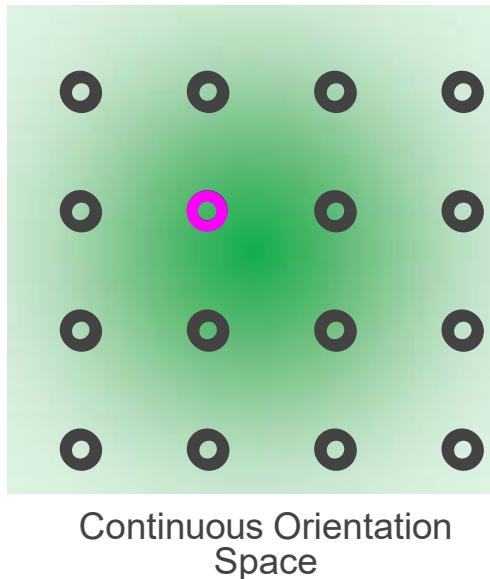
The robustness of spherical indexing doesn't mean you no longer have to prepare your samples well!!!



Orientation refinement

Orientation refinement: 2D example

Darker green
↓
Better model fit

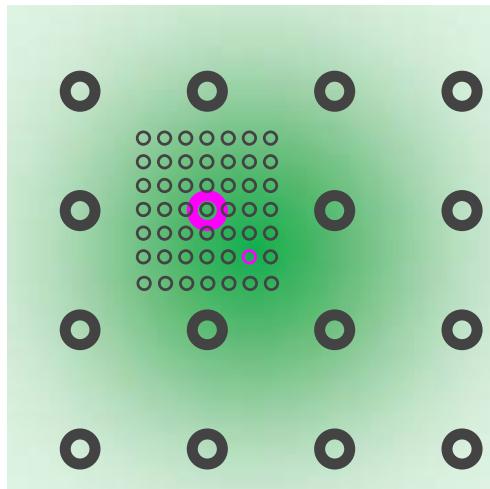


Refinement for increased angular precision

- No good match is found for too large of step size
- Too small of orientation step sizes are intractable
- Problem becomes intractable before desired precision

Orientation refinement: 2D example

Darker green
↓
Better model fit



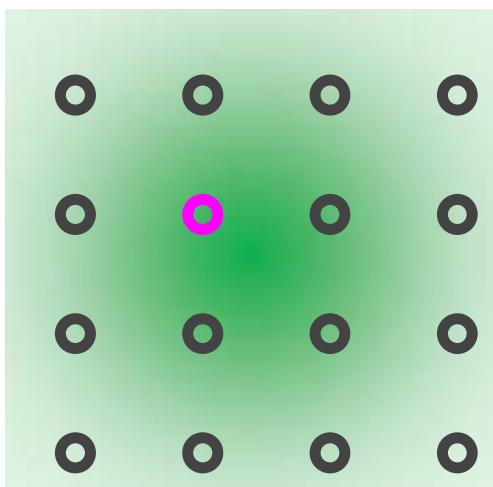
Realspace refinement

- No good match is found for too large of step size
- Too small of orientation step sizes are intractable
- Problem becomes intractable before desired precision
- Re-index using a high precision localized dictionary (in 3D)

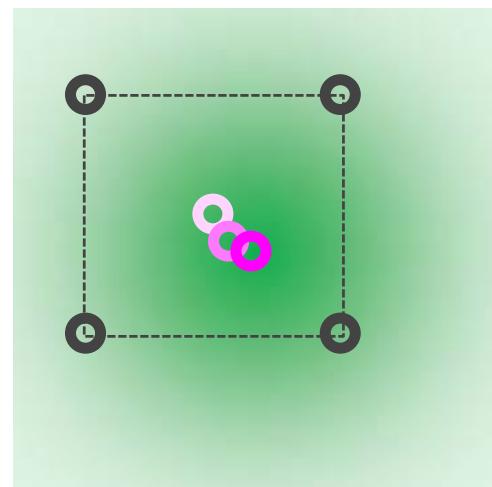
Orientation refinement: non-linear optimization example

Bound Optimization By Quadratic Approximation

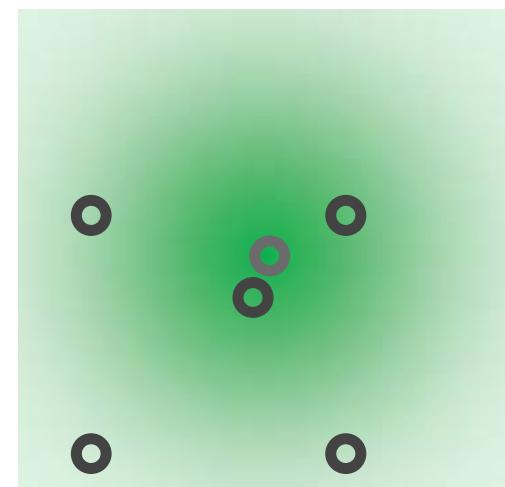
- Bounds are based on indexing grid
- Optimize to maximize normalized dot product
 - At each iteration choose a new iteration point by:
 - Fitting a Quadratic Approximation to the current points
 - Selecting the maxima of the quadratic constrained by the bounds



Initial bounding dot products



Estimate best point



Iterate until convergence

- Non-linear iterative optimization to refine orientation
- Bounded by specified dictionary parameters
- We are using a variant on the BOBYQA approach more suitable to EBSD

EL Pang, PM Larsen and CA Schuh (2020) "Global optimization for accurate determination of EBSD pattern centers" *Ultramicroscopy* **209**, 112876.
MJ Powell (2009) The BOBYQA algorithm for bound constrained optimization without derivatives. *Cambridge NA Report NA2009/06*, University of Cambridge, Cambridge, 26-46.

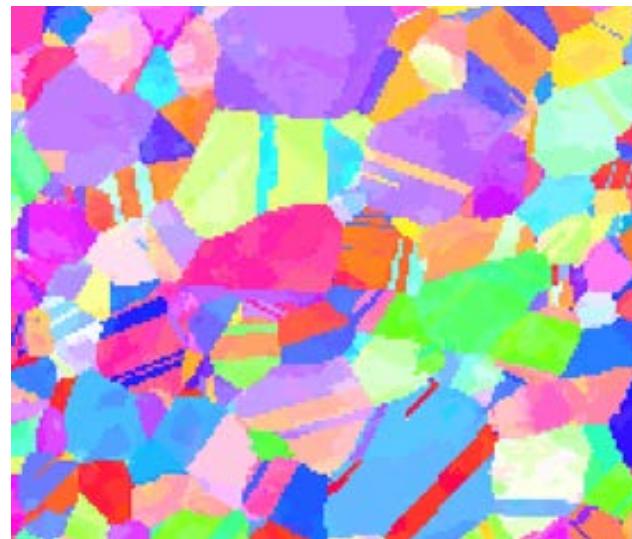
Realspace refinement

Hough Based



Continuous orientations

2.5° Dictionary



Discretized indexable orientations
before refinement

Refined

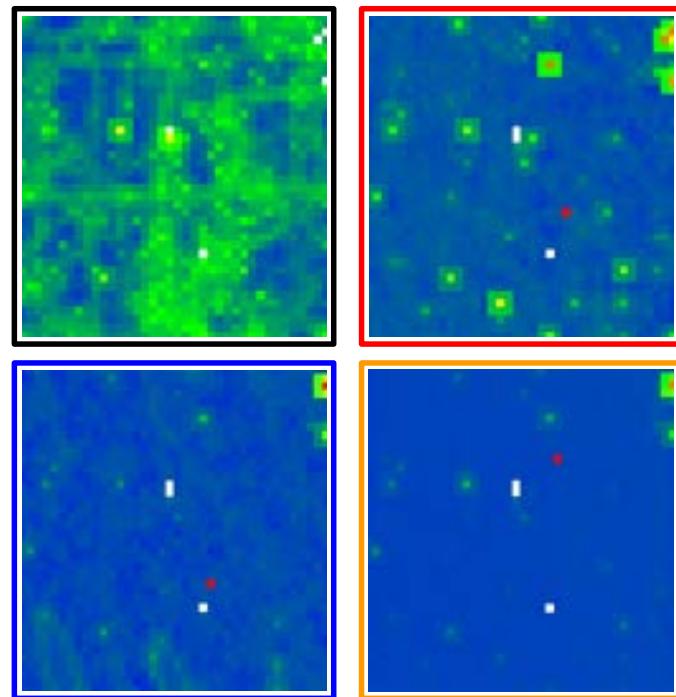
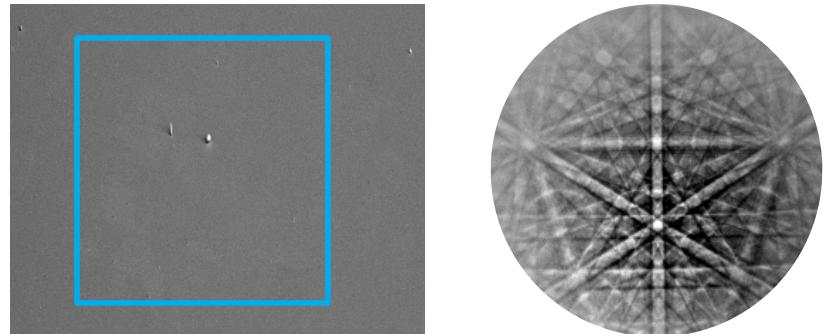
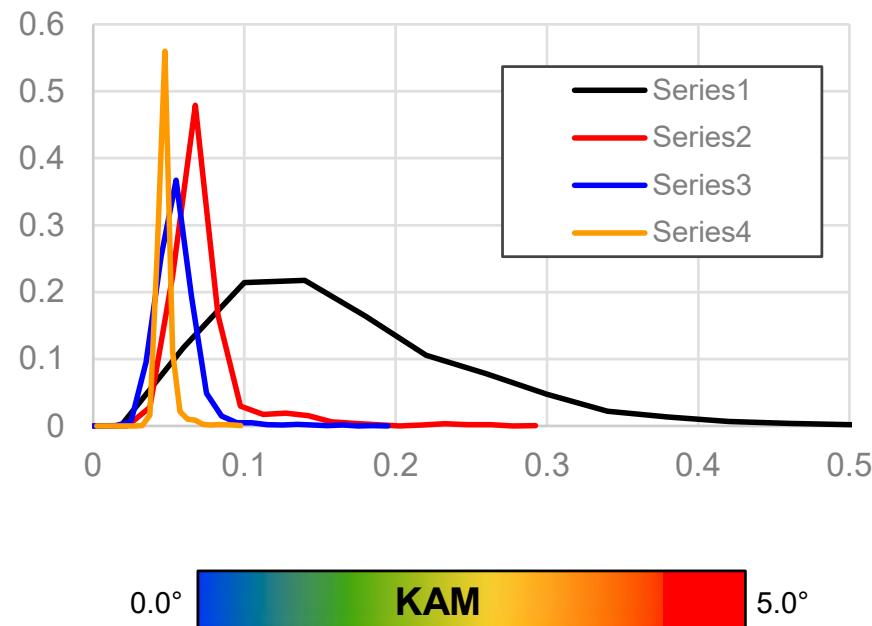


Continuous orientations after refinement

Increasing Bandwidth for Spherical Indexing

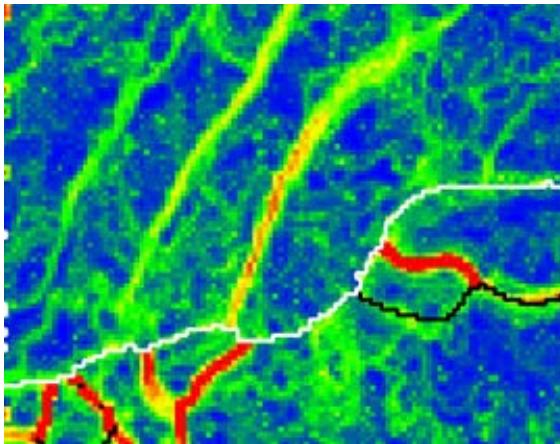
Preliminary precision tests

- Single crystal silicon
- 1 mm x 1 mm scan
- 480 x 480-pixel patterns
- 25-micron step size

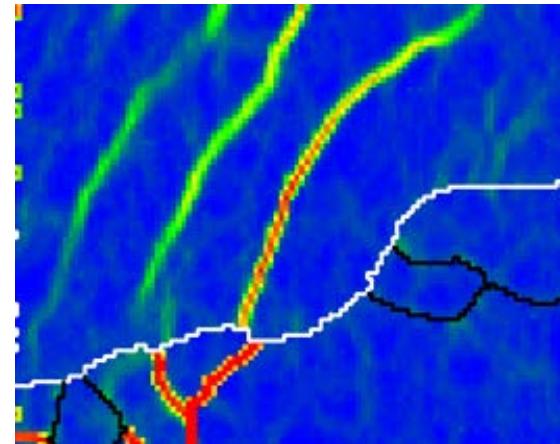


Cross-correlation comparison

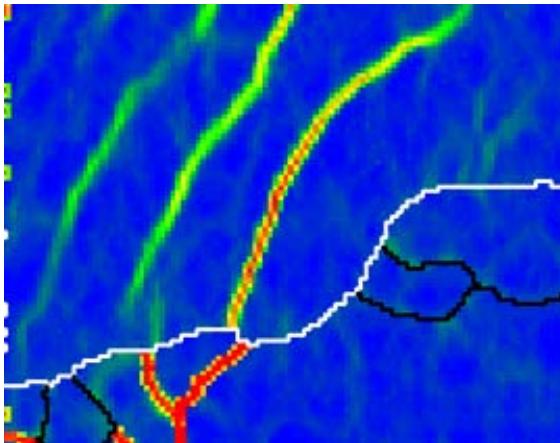
Hough



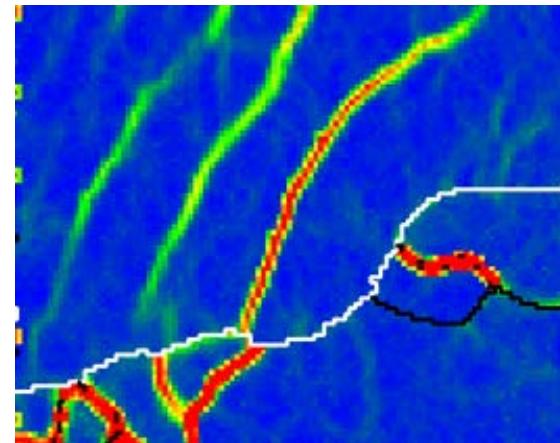
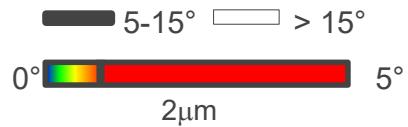
Hough + Refinement



Spherical + Refinement

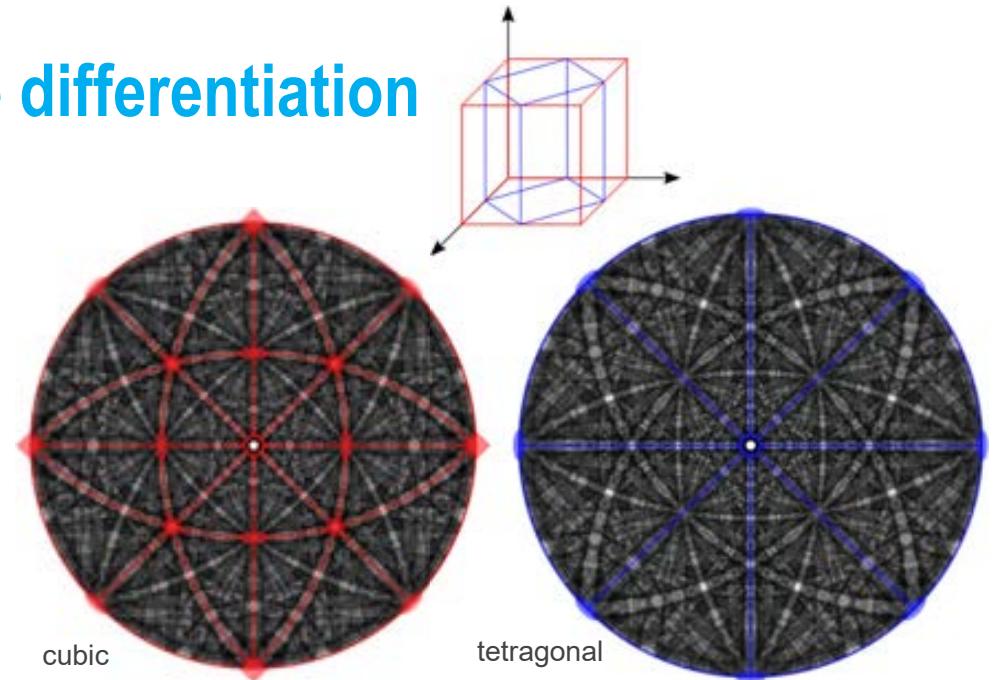


OpenXY
Courtesy Josh Kacher
Georgia Tech University



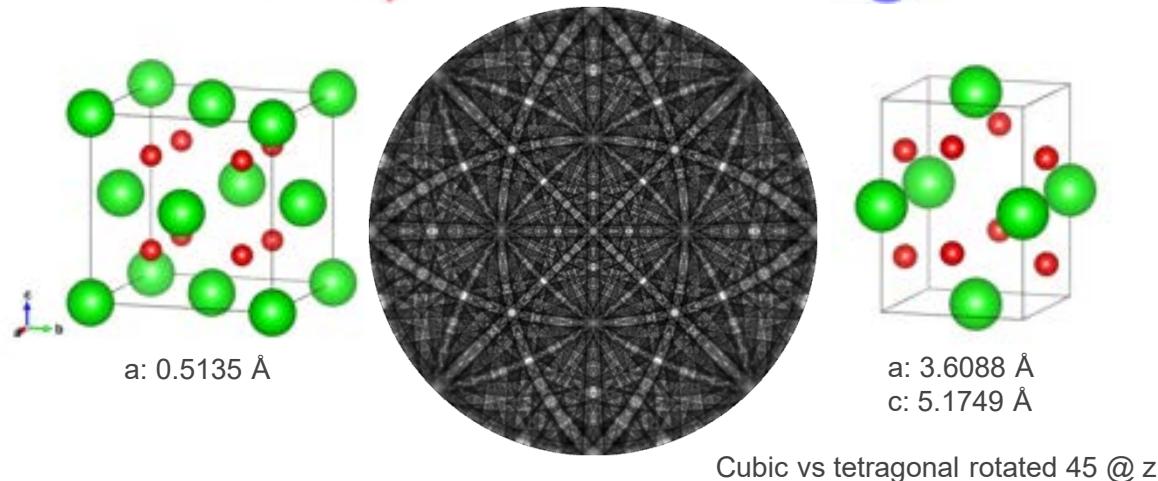
ZrO₂ pseudosymmetry & phase differentiation

- Tetragonal phase is small strain away from cubic
- Double cell c/a ratio 1.0134
- ~0.7% strain between phases
- Type and severity of pseudo symmetry is predicted well w/ spherical cross correlation

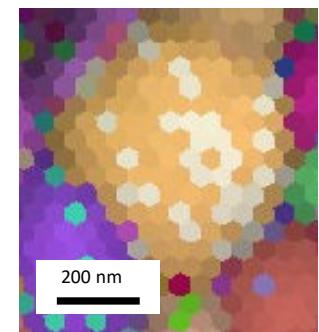


Normalized cross-correlation between the master patterns for each phase for all rotations

Max Cross Correlation	Cubic	Tetragonal
Cubic	60@<111> 29.9%	45@<001> 96.3%
Tetragonal		90@<110> 90.5%



ZrO₂ pseudosymmetry



Experimental Pattern

Tetragonal Orientation

Tetragonal Pseudosymmetric Orientation

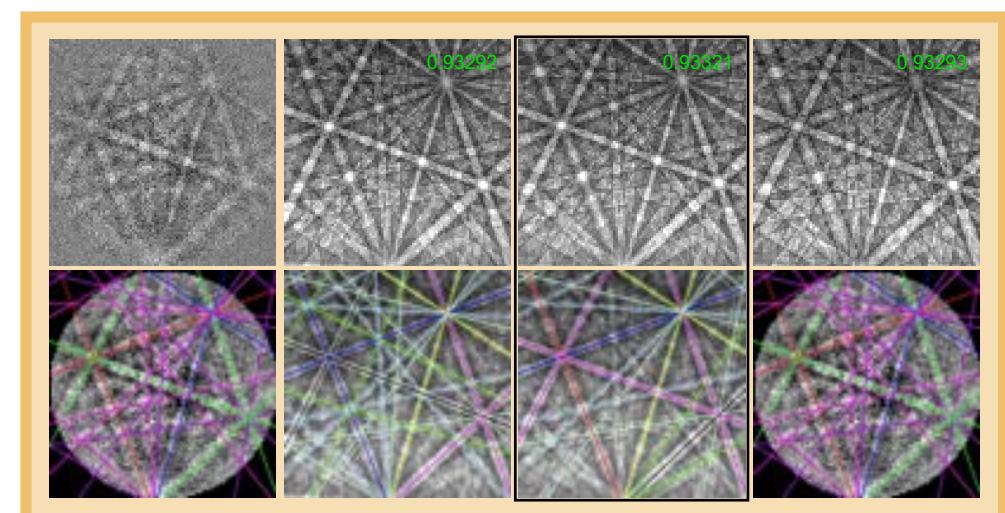
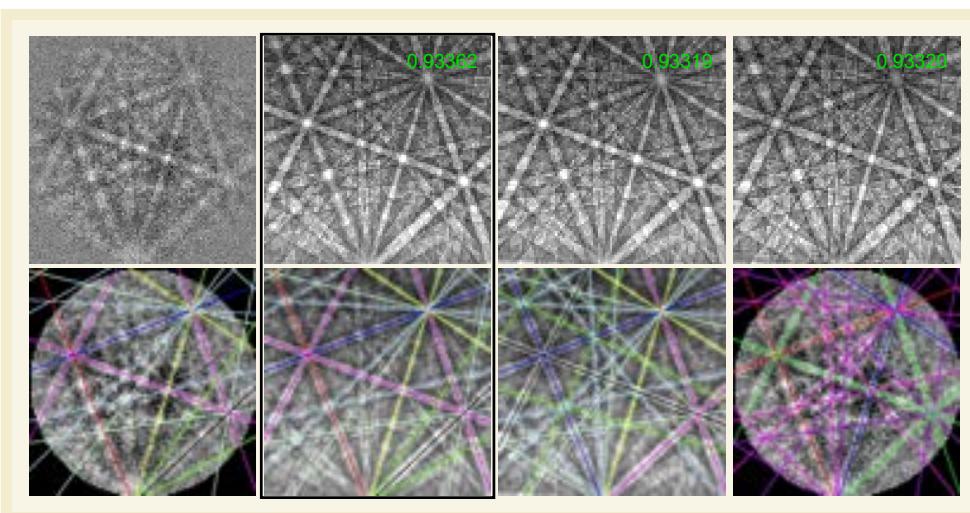
Cubic Orientation

Experimental Pattern

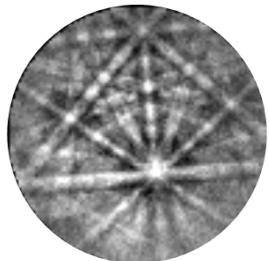
Tetragonal Orientation

Tetragonal Pseudosymmetric Orientation

Cubic Orientation



Pseudosymmetry / phase differentiation workflow

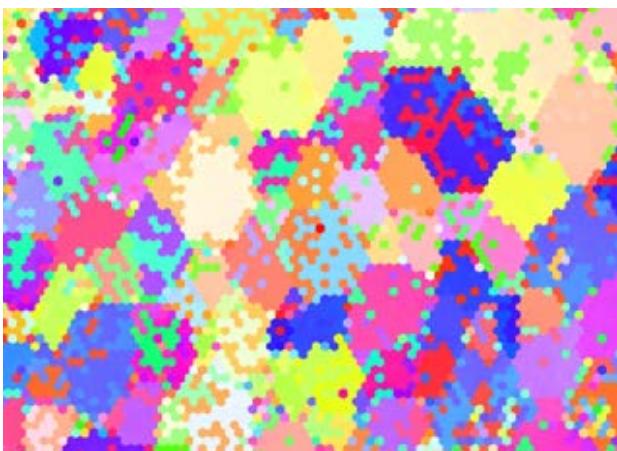


Experimental Pattern

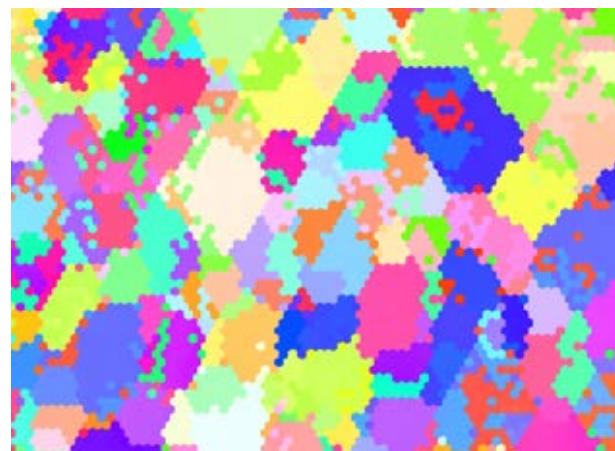
- Find the orientation with the highest normalized dot product (NDP) for the cubic phase (q_c)
 - Refine the cubic orientation (q_c^R)A red line graph showing a single sharp peak, representing the refined cubic orientation.
- Find the orientation with the highest NDP for the tetragonal phase -or-
- Calculate the tetragonal orientation related to the cubic orientation (q_t)
 - Refine the tetragonal orientation (q_t^R)A blue line graph showing a single sharp peak, representing the refined tetragonal orientation.
- Calculate the pseudosymmetric variation of q_t (q_{t2})
 - Refine q_{t2} (q_{t2}^R)A green line graph showing a single sharp peak, representing the refined pseudosymmetric variation.
- Select refined orientation with the maximum NDP

ZrO₂ tetragonal pseudosymmetry results

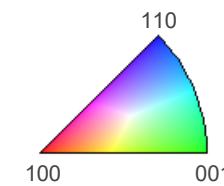
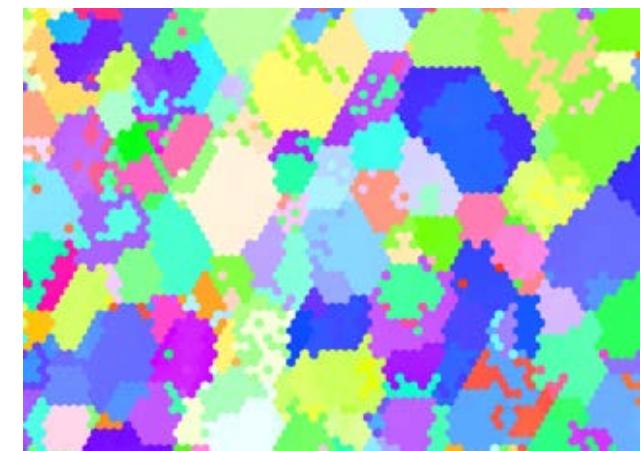
Hough



Spherical



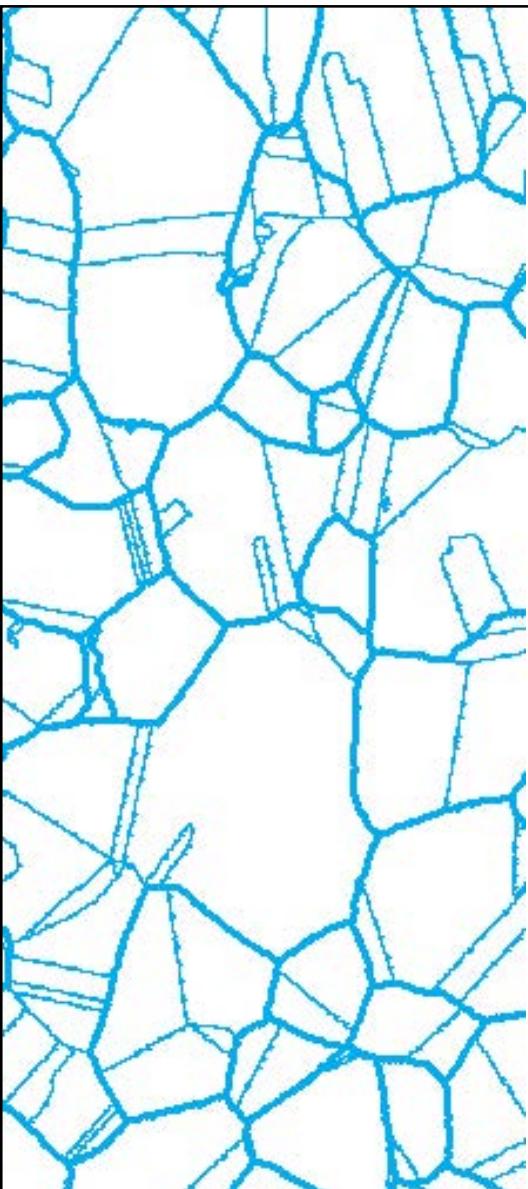
Spherical + Pseudosymmetry Analysis



Summary – orientation refinement

Refinement (OIM Matrix)

- Can start with Hough, DI, or SI results
- Improved angular resolution
 - Improved GNDs and KAMs
 - Rivaling HR-EBSD orientation precision (but no lattice distortion measurement)
- Master pattern and recorded patterns required
- Yet to explore:
 - Effects of pattern size and quality
 - Effects of lattice distortion (HR-EBSD)
 - ...



Thank you for your attention